

# CS 636: Testing of Concurrent Programs

**Swarnendu Biswas**

Department of Computer Science and Engineering,  
Indian Institute of Technology Kanpur

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# Evaluating Concurrent Programs

## **Functional correctness**

- Does the application compute what it is supposed to do?
- Check for concurrency errors such as atomicity violations, order violations, sequential consistency violations, deadlocks, and livelocks

## **Performance correctness**

- Does the application meet the performance requirements?
- Difficult to detect performance bottlenecks because of no failure symptoms
- Check for any performance regressions

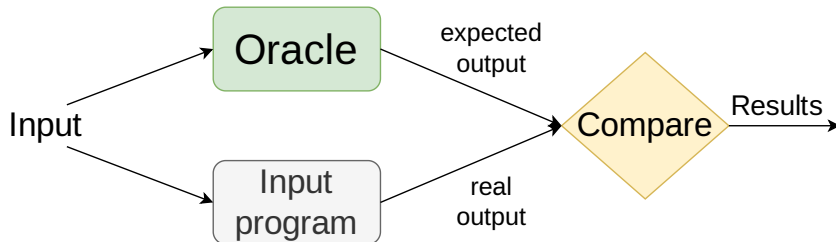
# Ideas to Ensure Correctness of Concurrent Programs

- Programming language features ensure bad things cannot happen by design (e.g., DPJ<sup>†</sup>)
  - Restricts the power and expressiveness of the language
- Design algorithms that are resilient to errors
  - Limits the kind of data structures that you can use
- Testing cannot guarantee correctness, usually a “best effort” strategy
  - + Places no restrictions on the application

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<sup>†</sup>Deterministic Parallel Java

# Software Testing



50% of my company employees are testers, and the rest spend 50% of their time testing!

– Bill Gates, 1995.

# Testing Concurrent Programs is Hard!

- Nondeterminism is everywhere
  - ▶ May be inherent in the application or can be due to inputs or interleavings
  - ▶ Large space of all possible thread interleavings
- Only specific thread interleavings may expose a concurrency bug (often called “Heisenbugs”)
  - ▶ Random or naïve testing can often miss such errors
- Even when found, errors are hard to debug
  - ▶ Usually no repeatable trace, just retrying the execution may not reproduce the error if it is rare
  - ▶ Debugging with `print` statements may actually change the desired buggy interleaving
  - ▶ Source of the bug may be far away from where it manifests
- Huge productivity problem
  - ▶ Developers and testers often spend weeks chasing after a single Heisenbug!

# High-level Requirements for Testing Concurrent Programs

- Test code, test inputs, and test oracles – a test harness
- A deterministic schedule may be needed to validate with the oracles
- Associated notion of coverage – test as many interleavings as possible

# Possibilities in Testing Concurrent Programs

1. Exhaustively explore all possible interleavings
2. Deterministic testing
  - ▶ Controls thread scheduling decisions during execution and systematically explores interleavings
  - ▶ Depends on a deterministic scheduler
  - ▶ Nondeterminism could still be there due to inputs
3. Nondeterministic “best effort” testing
  - ▶ Run the program for some time and hope for the best
  - ▶ Naïve and inefficient
4. Stress testing
  - ▶ Launch more threads than processors so that only a few threads are running at a time
  - ▶ Try to decrease predictability in thread interleavings
5. Noise injection
  - ▶ Introduce random perturbations during execution
  - ▶ Should not introduce false positives

# Alternatives to Testing

- Reason about correctness without running the program
  - ▶ Static analysis, Theorem proving, and Model checking
- Model checking checks whether a system model satisfies the given specification
  - ▶ Suffers from state explosion problem
  - ▶ Uses partial order reduction to deal with the state space problem
  - ▶ Use is limited to only critical portions of the program
- Sophisticated static analysis and model checking do not scale well
- Trying to prove programs correct requires a formal or mathematical characterization of the programs behavior
  - Very difficult for large systems since there are a lot of unknowns
    - For example, how do you model VM behavior like JIT compilation and GC?
  - ▶ Use is often limited to safety-critical software like integrated circuit design



# Address Nondeterminism

- Enforce the correct schedule that needs to be executed
  - ▶ Deterministic execution: record and replay
- Explore all possible schedules
  - ▶ Stateful exploration
    - Model the program state at each step and use backtrack and state comparison to explore new schedules
    - Advantage is it can merge same states, alleviating the state space explosion problem
    - Java Pathfinder is the state-of-art tool
  - ▶ Stateless exploration
    - Does not maintain program state
    - Each schedule maintains all the choices made during execution
    - Need to start from the beginning to execute other schedules
    - Each run is faster than stateful exploration, but possibly has more schedules to explore

# Software Testing vs Concurrency Testing

## Software Testing

- Broad area of work which considers the overall quality of the software along with the integrated engineering processes
  - ▶ Lots of paradigms, processes, and testing levels

## Concurrency Testing

- The context that we will be discussing has more narrow focus
  - ▶ Try to improve bug detection coverage of concurrent programs
  - ▶ Mostly carried out by the developers themselves during unit testing

# Software Testing vs Concurrency Testing

## Software Testing

- Broad area of work which considers the overall quality of the software along with the integrated engineering processes

- ▶
  - A concurrency bug manifests on a strict subset of possible schedules
    - ▶ Bugs that manifest in all schedules are not concurrency bugs
  - The problem of concurrency testing is to find those schedules that can trigger these bugs

## Concurrency Testing

- The context that we will be discussing has more narrow focus
  - ▶ Try to improve bug detection coverage of concurrent programs

# Current Practice in Concurrency Testing

- Concurrency testing is often delegated to random testing and stress testing
- Example: Test a concurrent queue implementation
  - ▶ Create numerous threads performing queue operations
  - ▶ Run for several hours
  - ▶ Randomly perturb the execution
- Stressing the system increases the likelihood of rare interleavings
  - ▶ Makes any error found hard to debug

# Performance Testing

- No good tools for predicting system performance
  - ▶ Check for latency, resource consumption
- Other considerations
  - ▶ Garbage Collection (GC) may take arbitrarily long and may be triggered at random points
    - Either turn off GC or design tests that invoke multiple GCs so that it can be averaged out
  - ▶ Dynamic compilation with JIT compiler
    - Methods compiled and time taken impacts the measured time of the program
    - Mixing interpretation and JIT is random
    - Fix which methods are going to be compiled beforehand and only compile those at runtime

# Related Directions

- Techniques to expose concurrency bugs<sup>§†</sup>
- Techniques to generate test cases (inputs) to trigger concurrency bugs
- Technique to automatically fix concurrency bugs<sup>‡¶</sup>
- ...

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<sup>§</sup>D. Wolff et al. Greybox Fuzzing for Concurrency Testing. ASPLOS'24.

<sup>†</sup>H. Zhao et al. Selectively Uniform Concurrency Testing. ASPLOS'25.

<sup>‡</sup>G. Jin et al. Automated Atomicity-Violation Fixing. PLDI'11.

<sup>¶</sup>H. Lin et al. PFix: Fixing Concurrency Bugs Based on Memory Access Patterns. ASE'18.

# Finding Concurrency Bugs Based on Code Patterns

# Insights Related to Concurrency Bugs

- Programmers make simple mistakes because of a tendency to think sequentially
- Natural tendency is to under-synchronize in pursuit of performance
  - ▶ Misconception that shared-memory synchronization is slow<sup>§</sup>
  - ▶ Lots of research to optimize the common case of low contention
- Indirect influence of the programming toolchain
  - + Writing threaded code with Java is comparatively easier
  - Java gives **limited** guarantees with improperly synchronized code unlike C and C++
    - You get type and memory safety, so why bother!!!

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<sup>§</sup>J. Preshing. Locks Aren't Slow; Lock Contention Is.



- Open-source static analysis tool for Java
- Goal is to use simple program analysis to find common patterns that indicate errors
  - ▶ Similar in spirit to automated code reviews
  - ▶ As such there can be both false negatives and false positives
  - ▶ Tries to minimize false positives using heuristics but cannot eliminate them completely
- Potential errors are classified into levels depending on estimated impact
- There is also a notion of confidence along with each reported error
- Lot of plugins are available for tools like Eclipse, IntelliJ, Ant, and Maven
- SpotBugs is a successor of FindBugs<sup>¶</sup>

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<sup>¶</sup>D. Hovemeyer and W. Pugh. Finding Concurrency Bugs in Java. PODC Workshop on Concurrency and Synchronization in Java Programs, 2004.

<sup>†</sup>SpotBugs: Find bugs in Java Programs

# Examples of Patterns Used in SpotBugs

- Synchronized set method, unsynchronized get method
- Finalizer method only nulling out fields
- Object pair operations with lock on only one object (e.g., equals() method)
- Double-checked locking

```
1 static SomeKls field;  
2 static SomeKls createSingleton() {  
3     if (field == null)  
4         synchronized (lock) {  
5             if (field == null) {  
6                 SomeKls obj = new SomeKls();  
7                 field = obj;  
8             }  
9         }  
10    return field;  
11 }
```

# Examples of Patterns Used in SpotBugs

- Unconditional wait
- Wait and notify without holding lock on the object, or two locks held while waiting
  - ▶ Intraprocedural analysis to identify lock scopes
- Spin wait on non-volatile data
- If overriding equals(), then hashCode() should be overridden too

```
1  if (!book.isReady()) {  
2      synchronized (book) {  
3          book.wait();  
4      }  
5  }
```

```
1  // non-volatile field  
2  while (listLock) {}
```

# Patterns Used in SpotBugs

Over 400 bug patterns divided into different categories

- All accesses to fields of a thread-safe class should be guarded with locks, otherwise are reported as bugs
  - ▶ Reduce false positives — ignore accesses in constructors and finalizers, ignore volatiles, final, and non-final public fields
- Ranks reports based on access frequency
  - ▶ 25% or fewer unsynchronized accesses is classified as medium to high priority
  - ▶ 25-50% unsynchronized accesses are classified as low priority

# Relevance of FindBugs/SpotBugs

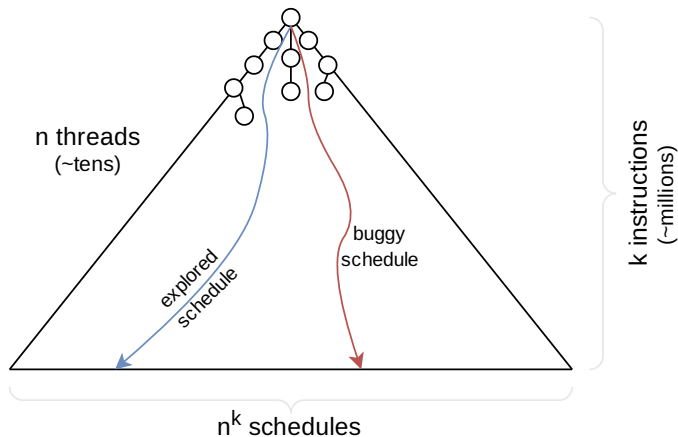
- An early work (~2004) that was very effective in pointing out errors in real applications like the Java libraries
  - ▶ Implementation is still being actively maintained

```
1 // From Eclipse 3.5RC3:  
2 // org.eclipse.update.internal.ui.views.FeatureStateAction:  
3  
4 if (adapters == null && adapters.length == 0)  
5     return;  
6  
7 // First seen in Eclipse 3.2  
8 // In practice, adapters is probably never null
```

# Probabilistic Concurrency Testing

# Exposing a Concurrency Bug with Random Testing

- Exposing a concurrency bug requires reproducing the correct interleaving
- No algorithm can find the bug with a probability greater than  $\frac{1}{n^k}$



# Debugging with Randomized Scheduling

Consider a naïve randomized scheduler that flips a coin in each step to decide which thread to schedule next

## Thread 1

```
1 assert(b != 0);  
2 step(1);  
3 step(2);  
4 ...  
5 ...  
6 step(m);  
7 a = 0;
```

## Thread 2

```
1 assert(a != 0);  
2 step(1);  
3 step(2);  
4 ...  
5 ...  
6 step(n);  
7 b = 0;
```



# Categorizing Concurrency Bugs

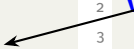
Bug depth is the number of ordering constraints that need to be satisfied to trigger the bug

## Thread 1

```
1 void init(...) {  
2     ...  
3     ...  
4     ...  
5     mThread = PR_CreateThread(mMain, ...);  
6     ...  
7 }
```

## Thread 2

```
1 ...  
2 void mMain() {  
3     mState=mThread->State;  
4     ...  
5 }  
6  
7
```



Mozilla: nsthread.cpp


# A Bug of Depth 1

## Parent

```
A: ...  
B: fork(child);  
C: p = malloc();  
D: ...  
E: ...
```

## Child

```
F: ...  
G: do_init();  
H: p->f++;  
I: ...  
J: ...
```



## Possible Schedules

ABCDEF <del>G</del> H <del>I</del> J	✓
ABF <del>G</del> H <del>C</del> DEI <del>J</del>	✗
ABF <del>G</del> CDEH <del>I</del> J	✓
ABF <del>G</del> CHDEI <del>J</del>	✓
ABF <del>G</del> H <del>I</del> J <del>C</del> DE	✗

...

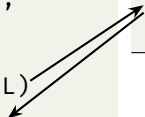
# A Bug of Depth 2

## Parent

```
A: ...  
B: p = malloc();  
C: fork(child);  
D: ...  
E: if (p != NULL)  
F:   p->f++;  
G:
```

## Child

```
H: ...  
I: p = NULL;  
J: ...
```



## Possible Schedules

ABCDEF <b>GHIJ</b>	✓
ABCDE <b>H</b> IJFG	✗
AB <b>CH</b> IDE <b>GJ</b>	✓
ABCD <b>H</b> E <b>F</b> I <b>J</b> G	✓
AB <b>CH</b> DEI <b>J</b> FG	✗
...	

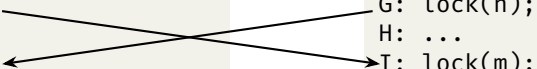
# Another Bug of Depth 2

Parent

```
A: ...  
B: lock(m);  
C: ...  
D: lock(n);  
E: ...
```

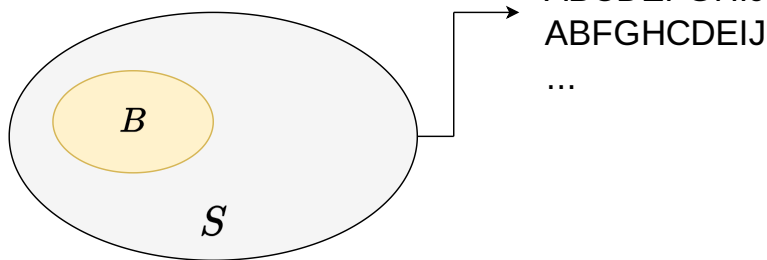
Child

```
F: ...  
G: lock(n);  
H: ...  
I: lock(m);  
J: ...
```



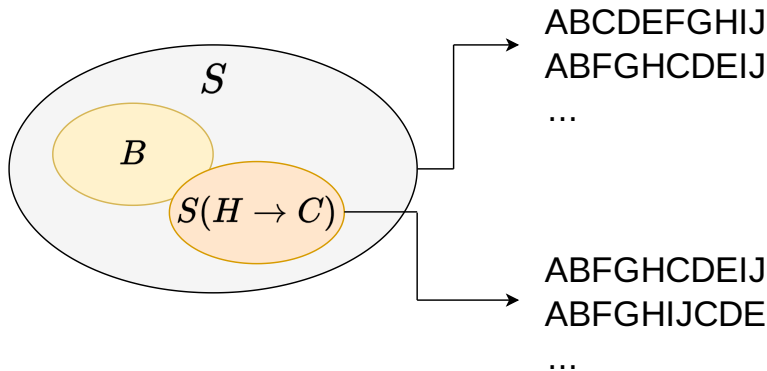
# What is Bug Depth?

- A system is defined by its set of executions  $S$
- Each execution is a sequence of labeled events
- A concurrency bug  $B$  is some **strict** subset of  $S$



# What is Bug Depth?

- An ordering constraint  $c$  is a pair of events  $c = (a \rightarrow b)$
- A schedule  $s \in S$  satisfies  $(a \rightarrow b)$  if  $a$  occurs before  $b$  in  $s$
- Let  $S(c_1, c_2, \dots, c_d)$  be the set of schedules that satisfy constraints  $c_1, c_2, \dots, c_d$

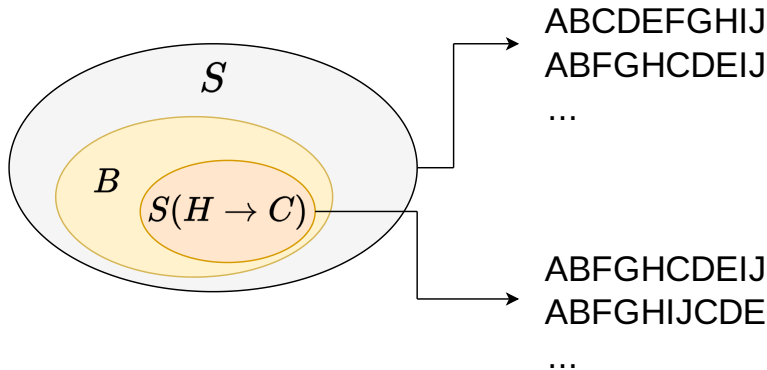


# What is Bug Depth?

A bug depth is  $d$  if there exists constraints  $c_1, c_2, \dots, c_d$  such that

$$S(c_1, c_2, \dots, c_d) \subseteq B$$

and  $d$  is the smallest such number for  $B$

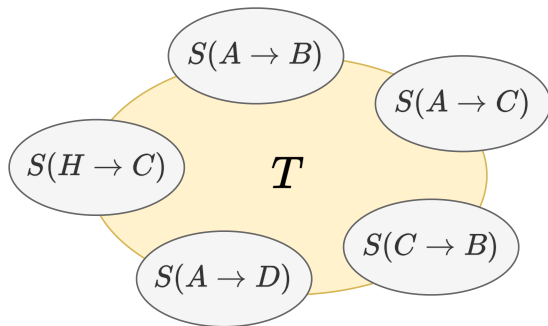


# Finding All Bugs of Depth $d$

- A set of schedules  $T$  covers all bugs of depth  $d$  if

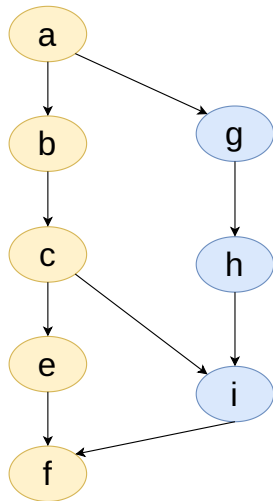
$$\forall c_1, c_2, \dots, c_d : S(c_1, c_2, \dots, c_d) \cap T \neq \emptyset$$

- The coverage problem is to find the smallest such  $T$



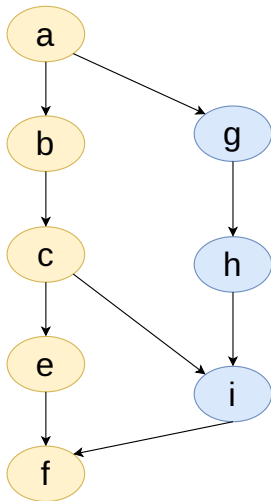


## Concurrent Interleavings when $d = 1$

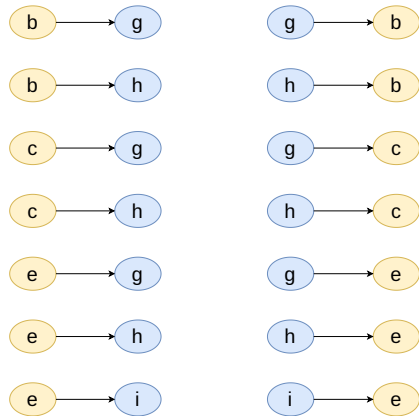


Which pair of operations are concurrent?

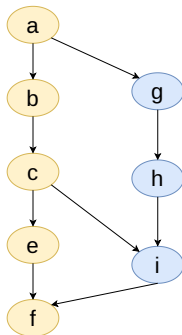
# Concurrent Interleavings when $d = 1$



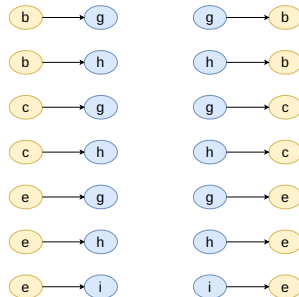
Need to cover all



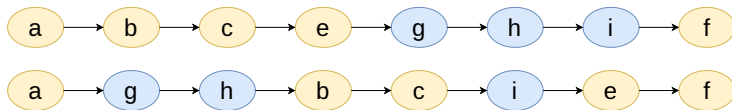
# Concurrent Interleavings when $d = 1$



Need to cover all



Two interleavings are sufficient!



# Concurrency Bugs and Bug Depth

- Most concurrency bugs are usually of **low** depth
  - Order violations depth 1 (or 2 in presence of control flow)
  - Atomicity violations depth 2
  - Deadlocks depth 2 if 2 threads are involved, depth  $n$  if  $n$  threads are involved
- Bugs with greater depth are harder to expose

# A Bug of Depth 2

## Main Thread

```
1 ...  
2 free(mutex);  
3  
4 exit(0);  
5 ...
```

## Filewriter Thread

```
1 ...  
2  
3 mutex.unlock();  
4  
5 ...
```


# An Ordering Bug of Depth 2

## Main Thread

```
1 ...  
2 init = true;  
3 t = new T();  
4 ...  
5 ...
```

## Filewriter Thread

```
1 ...  
2 ...  
3 if (init)  
4   t->state = 1;  
5 ...
```



Presence of control dependence may complicate the interleaving

# PCT: Probabilistic Concurrency Testing

- PCT is an intelligent randomized scheduler for finding concurrency bugs
- PCT aims to correctly schedule instructions relevant to expose a bug, irrelevant instructions are ignored to reduce the search space
- Provides probabilistic guarantees to expose bugs
  - ▶ Every run finds every bug with nontrivial probability
  - ▶ Repeated test runs increases the chance of finding a bug

# PCT's Randomized Scheduler

- User-level scheduler is randomized and priority-based
  - ▶ Every thread has a priority, lower number indicates lower priority
- Only one thread is scheduled to execute at each step
- Low priority threads are scheduled only when higher-priority threads are blocked
- A dynamic execution has a few priority change points
  - ▶ Priority change points have fixed priorities assigned
  - ▶ A thread that reaches a change point will inherit the priority of the change point



# PCT Algorithm

**Input**  $n$  threads,  $k$  instructions, and  $d$  priority change points

- Steps**
- (i) Assign  $n$  priority values  $d, d + 1, \dots, d + n - 1$  randomly to the  $n$  threads
  - (ii) Pick  $d - 1$  random priority change points from the  $k$  instructions. Each change point  $k_i, 1 \leq i < d$ , has an associated priority of  $i$ .
  - (iii) Schedule threads based on their priorities. The highest priority thread that is enabled runs for one step.
  - (iv) When a thread reaches change point  $k_i$ , change the priority of that thread to  $i$

Higher priority threads run faster

An ordering constraint ( $a \rightarrow b$ ) will be met if  $a$  is executed by a higher priority thread

# How PCT Works?

Thread 1

1

```
1 ...  
2 t = new T();  
3 ...  
4  
5
```

Thread 2

2

```
1 ...  
2  
3 if (t->state == 1)  
4 ...  
5
```

initial thread  
priority

# How PCT Works?

Thread 1

2

```
1 ...  
2 x = NULL;  
3 ...  
4  
5
```

Thread 2

3

```
1 ...  
2 if (x != NULL)  
3  
4 x->print();  
5
```

priority change  
point

1

# How PCT Works?

Thread 1

3

```
1 ...  
2 lock(a);  
3 ...  
4 lock(b);  
5 ...
```

1

Thread 2

2

```
1 ...  
2 lock(b);  
3 ...  
4 lock(a);  
5 ...
```

# Issues to Consider in PCT

- Does not reuse OS thread priorities
  - ▶ PCT implements a user-level scheduler instead
  - ▶ Needs to force higher priority threads to run faster
- Consider priority inversion in presence of multiple threads
  - ▶ Higher priority thread may be blocked for a resource owned by a lower priority thread violating PCT's assumptions
    - Assume that Thread 2 needs to run before Thread 1 to expose a bug
    - Thread 1 has a lower priority than Thread 2, but Thread 2 is blocked on a resource held by Thread 3 which has the lowest priority
  - ▶ But there will be other schedules where the priorities will be in the correct order with probability  $\frac{1}{n}$
- Ensure starvation freedom
  - ▶ Repeatedly slowing down the low-priority thread can cause starvation or timeout
  - ▶ Higher priority threads may wait in a spin loop for a lower priority thread
  - ▶ Uses heuristics to identify and resolve such situations

# Effectiveness of PCT

- Probability of finding any bug with depth  $d$  in PCT is not less than  $\frac{1}{nk^{(d-1)}}$ 
  - ▶ Contrast with the probability of naïve random testing which is  $\frac{1}{n^k}$
- If  $d = 1$  or  $d = 2$  (common cases), then probabilities of finding a bug is  $\frac{1}{n}$  and  $\frac{1}{nk}$ , respectively
- PCT is empirically expected to do better than the worst-case bound

Why?

# Effectiveness of PCT

- Probability of finding any bug with depth  $d$  in PCT is  $\frac{1}{nk^{(d-1)}}$ 
  - ▶ Contrast with the probability of naïve random testing which is  $\frac{1}{n^k}$
- If  $d = 1$  or  $d = 2$  (common cases), then probabilities of finding a bug is  $\frac{1}{n}$  and  $\frac{1}{nk}$ , respectively
- PCT
  - Good enough to have the priority change point on one from a set of instructions, need not be exact
  - Multiple ways to trigger a bug (e.g., symmetric case in deadlocks)
  - Buggy code can be repeated multiple times in a program/test



# Extensions of PCT

- PCT runs only a single thread at a time
  - Does not utilize multicore hardware, incurs large slowdowns
- PPCT: Parallel PCT
  - ▶ Insight: Need to control the schedule of only  $d$  threads to expose a bug of depth  $d$
  - ▶ Partitions threads into high ( $> d$ ) and low priority
  - ▶ Runs threads with higher priority parallelly, size of the lower priority set is bounded by  $d$
  - ▶ PCT serializes all threads, PPCT serializes only the low priority threads

# PPCT Algorithm

**Input**  $n$  threads,  $k$  instructions, and  $d$  priority change points

- Steps**
1. Pick a random thread and assign it a priority  $d$ . Insert the thread in a low priority set  $L$ . Insert all other threads into a high priority set  $H$ .
  2. Pick  $d - 1$  random priority change points from the  $k$  instructions. Each change point  $k_i, 1 \leq i < d$  has an associated priority of  $i$ .
  3. At each scheduling step, schedule any non-blocked thread in  $H$ . If  $H$  is empty or if all threads in  $H$  are blocked, then schedule the highest priority thread in  $L$ .
  4. When a thread reaches change point  $k_i$ , change the priority of that thread to  $i$  and insert in  $L$ .

# CHESS: Systematic Schedule Exploration

# What have we learnt so far?

- Systematic schedule exploration enumerates all possible thread interleavings
  - ▶ Does not scale
- PCT and PPCT argued in favor of intelligent randomized testing

CHES performs systematic schedule exploration

# Traditional Testing

```
1 testStartup();  
2 while (true) {  
3     runTestScenario();  
4     if (*some condition*)  
5         break;  
6 }  
7 testShutdown();
```

# What is required for systematic exploration?

- Suppose you have two threads contending on a lock
- Systematic exploration should explore both schedules — one where each thread wins the lock first

Basically capture all nondeterministic choices

# Why Track Nondeterminism?

## Capture all sources of nondeterminism

- For example, input, environment, interleaving, and other sources like compiler and hardware reordering

## Allows exploring these nondeterministic choices

Required for reliably reproducing errors

# Input Nondeterminism

- Environment data can affect program execution
  - ▶ User can provide different inputs or the program can receive network packets with different contents
  - ▶ Nondeterministic functions like `gettimeofday()` and `random()`
- Idea: Use “record and replay” techniques
  - ▶ Two phases — a record phase and a replay phase
  - ▶ Which phase is usually more expensive, record or replay?



# Capturing Input Nondeterminism in CHES

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- CHES is not a typical record-and-replay system
- Relies on the test setup to provide deterministic inputs
- Records a few nondeterministic events like current time, processor and thread ID mapping, and random numbers

# Concurrent Executions are Nondeterministic

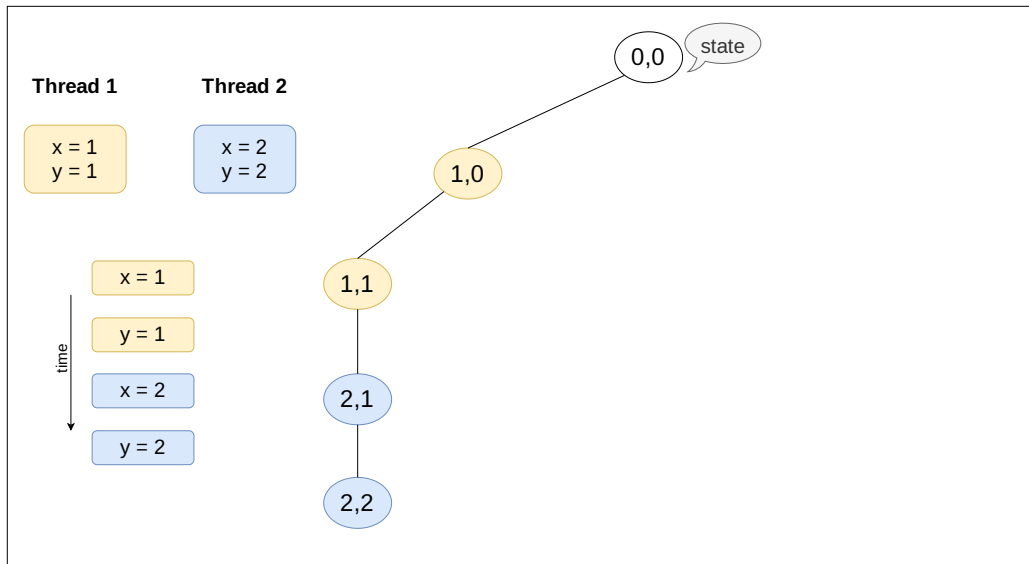
**Thread 1**

$x = 1$   
 $y = 1$

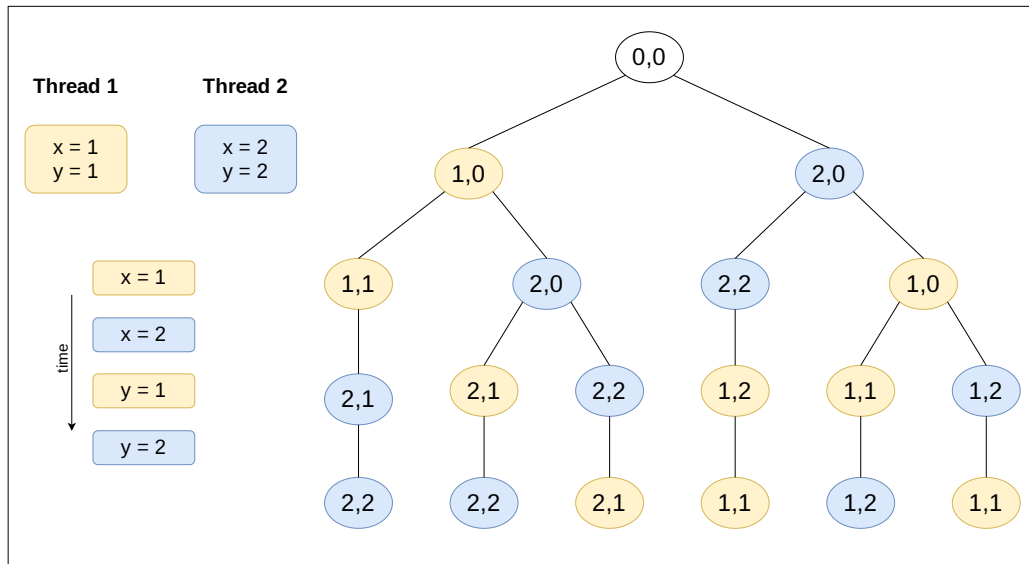
**Thread 2**

$x = 2$   
 $y = 2$

# Concurrent Executions are Nondeterministic



# Concurrent Executions are Nondeterministic



# Scheduling Nondeterminism

## 💡 Interleaving nondeterminism

- Threads can race to access shared variables or monitors
- OS can preempt threads at arbitrary points

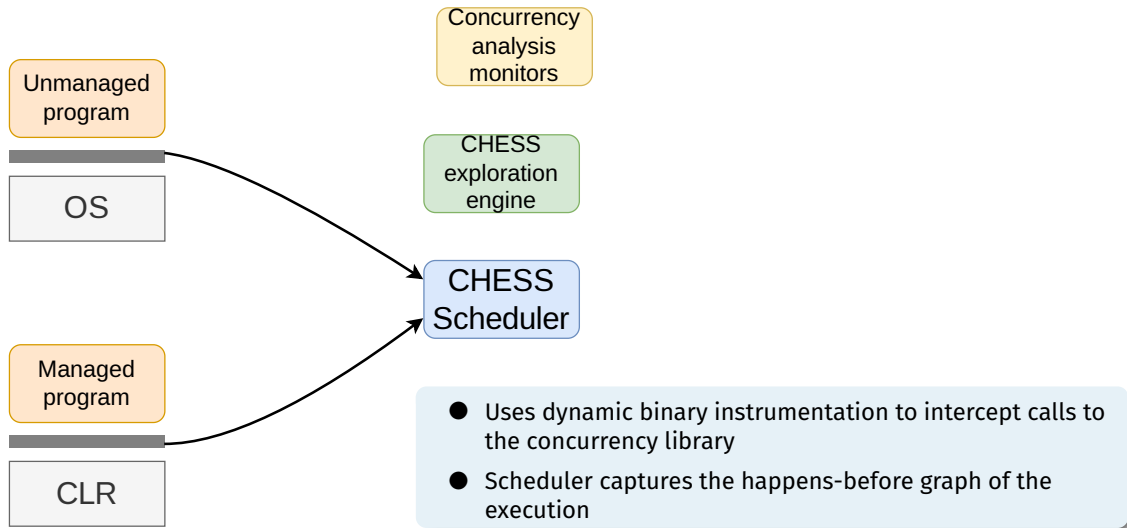
## 💡 Timing nondeterminism

- Timers can fire in different orders
- Sleeping threads wake up at arbitrary times in the future
- Asynchronous calls complete at arbitrary times in the future

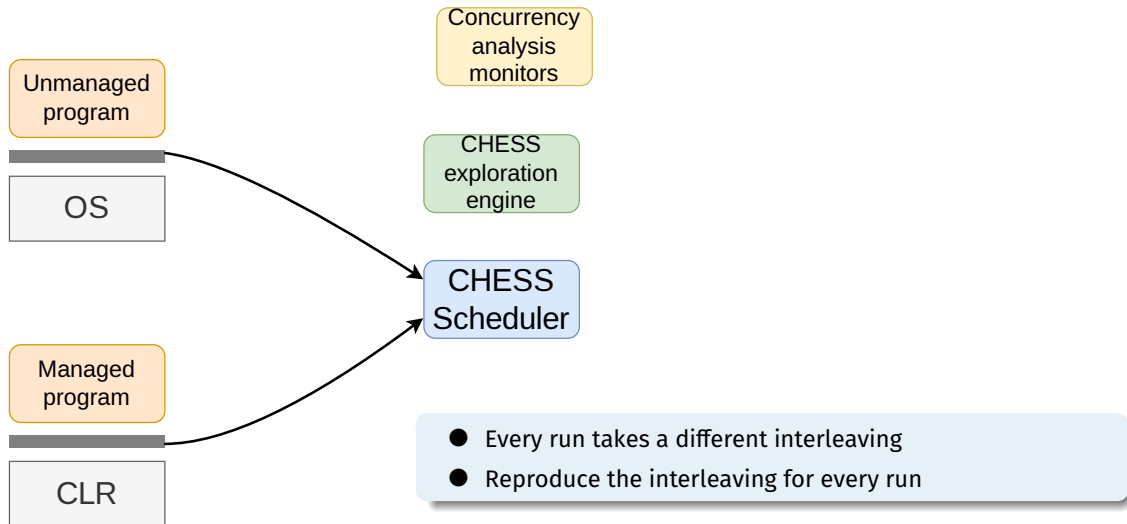
# CHESS in a nutshell

- User-mode scheduler — controls all scheduler nondeterminism
- Provides systematic overage of all thread interleavings
  - ▶ Every program run takes a different thread interleaving
- CHESS is precise, does not introduce new behaviors
- Provides replay capability for easy debugging
  - ▶ Reproduce the interleaving for every run

# CHESS Architecture



# CHESS Architecture





# Interleaving Nondeterminism

```
balance = 100;
```

## Deposit Thread

```
1 void Deposit100() {  
2     EnterCriticalSection(&cs);  
3     balance += 100;  
4     LeaveCriticalSection(&cs);  
5 }
```

## Withdrawal Thread

```
1 void Withdraw100() {  
2     EnterCriticalSection(&cs);  
3     int t = balance;  
4     LeaveCriticalSection(&cs);  
5  
6     EnterCriticalSection(&cs);  
7     balance = t - 100;  
8     LeaveCriticalSection(&cs);  
9 }
```

```
assert(balance == 100);
```

# Invoke the Scheduler at Preemption Points

```
balance = 100;
```

## Deposit Thread

```
1 void Deposit100() {  
2     ChessSchedule();  
3     EnterCriticalSection(&cs);  
4     balance += 100;  
5     ChessSchedule();  
6     LeaveCriticalSection(&cs);  
7 }
```

Each call is a potential  
preemption point

## Withdrawal Thread

```
1 void Withdraw100() {  
2     ChessSchedule();  
3     EnterCriticalSection(&cs);  
4     int t = balance;  
5     ChessSchedule();  
6     LeaveCriticalSection(&cs);  
7     ChessSchedule();  
8     EnterCriticalSection(&cs);  
9     balance = t - 100;  
10    ChessSchedule();  
11    LeaveCriticalSection(&cs);  
12 }
```

```
assert(balance == 100);
```

# Insert Predictable Delays with Additional Synchronization

## Deposit Thread

```
1 void Deposit100() {  
2  
3  
4  
5  
6     waitEvent(e1);  
7     EnterCriticalSection(&cs);  
8     balance += 100;  
9     LeaveCriticalSection(&cs);  
10    setEvent(e2);  
11 }
```

## Withdrawal Thread

```
1 void Withdraw100() {  
2     EnterCriticalSection(&cs);  
3     int t = balance;  
4     LeaveCriticalSection(&cs);  
5     setEvent(e1);  
6  
7  
8  
9  
10  
11  
12     waitEvent(e2);  
13     EnterCriticalSection(&cs);  
14     balance = t - 100;  
15     LeaveCriticalSection(&cs);  
16 }
```

# Blindly Inserting Delays can lead to Deadlocks!

## Deposit Thread

```
1 void Deposit100() {  
2  
3  
4  
5  
6     EnterCriticalSection(&cs);  
7     balance += 100;  
8     waitEvent(e1);  
9     LeaveCriticalSection(&cs);  
10 }
```

## Withdrawal Thread

```
1 void Withdraw100() {  
2     EnterCriticalSection(&cs);  
3     int t = balance;  
4     LeaveCriticalSection(&cs);  
5     setEvent(e1);  
6  
7  
8  
9  
10  
11     EnterCriticalSection(&cs);  
12     balance = t - 100;  
13     LeaveCriticalSection(&cs);  
14 }
```



# CHESS Scheduler Basics

- CHESS is a non-preemptive, fair, round-robin and priority-based, starvation-free scheduler
  - ▶ Executes chunks of code atomically
- Scheduler basically captures the happens-before graph for the execution
- Each graph node tracks threads, synchronization resources, and the operations, and whether tasks are enabled or disabled
- Introduces an event per thread, every thread blocks on its event
- The scheduler wakes one thread at a time by enabling the corresponding event
- The scheduler does not wake up a disabled thread
  - ▶ Need to know when a thread can make progress
  - ▶ Synchronization wrappers provide this information
- The scheduler has to pick one of the enabled threads
  - ▶ The exploration engine decides for the scheduler

## Three Steps

**Record** Schedules a thread till the thread yields

**Replay** Replays a sequence of scheduling choices from a trace file

**Search** Uses the enabled information at each schedule point to determine the scheduler for the next iteration

# Traditional Testing vs CHES

## Traditional Testing

```
1 testStartup();
2 while (true) {
3
4     runTestScenario();
5
6
7     if (some condition)
8         break;
9
10 }
11 testShutdown();
```

## CHES

```
1 testStartup();
2 while (true) {
3
4     runTestScenario();
5
6
7     if (some condition)
8         break;
9
10 }
11 testShutdown();
```

The CHES diagram includes three callout bubbles: a yellow bubble labeled "replay" pointing to line 4, a yellow bubble labeled "record" pointing to line 5, and a yellow bubble labeled "search" pointing to line 9.

# Preemption bounding

- Systematically inserts a small number of preemptions
- Preemptions are context switches forced by the scheduler (e.g., timeslice expiration)
- Non-preemptions – a thread voluntarily yields (e.g., blocking on an unavailable lock and thread end)

## Thread 1

```
1 x = 1;  
2 if (p != nullptr) {  
3     x = p->f;  
4 }
```

## Thread 2

```
1  
2 p = nullptr;  
3  
4
```



# Preemption bounding

- Systematically inserts a small number of preemptions
- Preemptions are context switches forced by the scheduler (e.g., timeslice expiration)
- Non-preemptions – a thread voluntarily yields (e.g., blocking on an unavailable lock and thread end)

## Thread 1

```
1 x = 1;  
2 if (p != nullptr) {  
3     ...  
4     x = p->f;  
5 }  
6  
7
```

preempted

## Thread 2

```
1  
2  
3  
4 p = nullptr;  
5  
6  
7
```

# Preemption bounding

- Systematically inserts a small number of preemptions
- Preemptions are context switches forced by the scheduler (e.g., timeslice expiration)
- Non-preemptions – a thread voluntarily yields (e.g., blocking on an unavailable lock and thread end)

Thread 1

Helps alleviate the problem of state space explosion

```
1 x = 1;  
2 if (p != nullptr) {  
3     ...  
4     ...  
5     x = p->f;  
6 }  
7
```

preempted

Thread 2

```
2  
3  
4 p = nullptr;  
5  
6  
7
```

# Advantages of preemption bounding

- Most errors are caused by few ( $<2$ ) preemptions (similar to bug depth)
- Generates an easy to understand error trace
  - ▶ Preemption points almost always point to the root cause of the bug
- Leads to good heuristics
  - ▶ Insert more preemptions in code that needs to be tested
  - ▶ Avoid preemptions in libraries
  - ▶ Insert preemptions in recently modified code
- A good coverage guarantee to the user
  - ▶ When CHES finishes exploration with 2 preemptions, any remaining bug requires 3 preemptions or more

# Contributions of CHESS

Integrates stateless model checking ideas to testing concurrent programs with minimal perturbation

Ability to consistently reproduce erroneous interleavings

# DTHREADS: Efficient and Deterministic Multithreading

# Remember the Sources of Nondeterminism?

---

Sources of nondeterminism: input, environment, interleaving, other sources like compiler and hardware reordering

# Deterministic Multithreading

- Deterministic execution can simplify multithreading
  - ▶ Executing the same program with same inputs will always provide same results
- Deterministic multithreading would simplify
  - ▶ Testing and debugging
  - ▶ Record and replay mechanism
  - ▶ Fault tolerance mechanisms

# Different Interleavings are Possible

```
1  int a = 0;
2  int b = 0;
3  int main() {
4      pthread_create(&p1, NULL, thread1, NULL);
5      pthread_create(&p2, NULL, thread2, NULL);
6      pthread_join(&p1, NULL);
7      pthread_join(&p2, NULL);
8      printf("%d, %d\n", a, b);
9  }
```

What are possible outputs?

```
14 void* thread1(void*) {
15     if (b == 0) {
16         a = 1;
17     }
18     return NULL;
19 }
20
21 void* thread2(void*) {
22     if (a == 0) {
23         b = 1;
24     }
25     return NULL;
26 }
```



# Guarantees by DTHREADS

---

- DTHREADS guarantees deterministic execution of multithreaded programs even in the presence of data races
- Given the same sequence of inputs or OS events, a program using DTHREADS always produces the same output
- DTHREADS allows interleavings only at synchronization points
- DTHREADS uses synchronization operations as transactional boundaries
- Changing the code or input does not affect the schedule as long as the sequence of synchronization operations remains unchanged

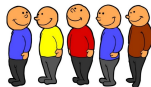
# How DTHREADS Provides Determinism



Isolation



Deterministic time



Deterministic order

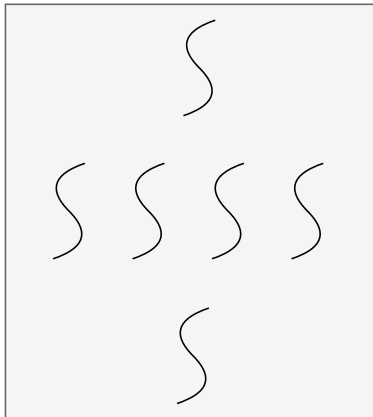
# Deterministic Execution by DTHREADS

```
1  int a = 0;
2  int b = 0;
3  int main() {
4      pthread_create(&p1, NULL, thread1, NULL);
5      pthread_create(&p2, NULL, thread2, NULL);
6      pthread_join(&p1, NULL);
7      pthread_join(&p2, NULL);
8      printf("%d, %d\n", a, b);
9  }
```

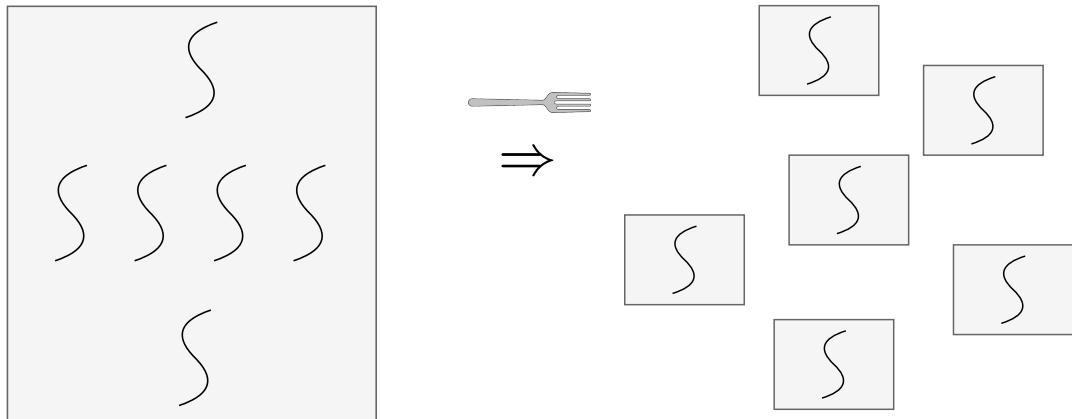
DTHREADS will always generate (1, 1)  
as the output

```
14 void* thread1(void*) {
15     if (b == 0) {
16         a = 1;
17     }
18     return NULL;
19 }
20
21 void* thread2(void*) {
22     if (a == 0) {
23         b = 1;
24     }
25     return NULL;
26 }
```

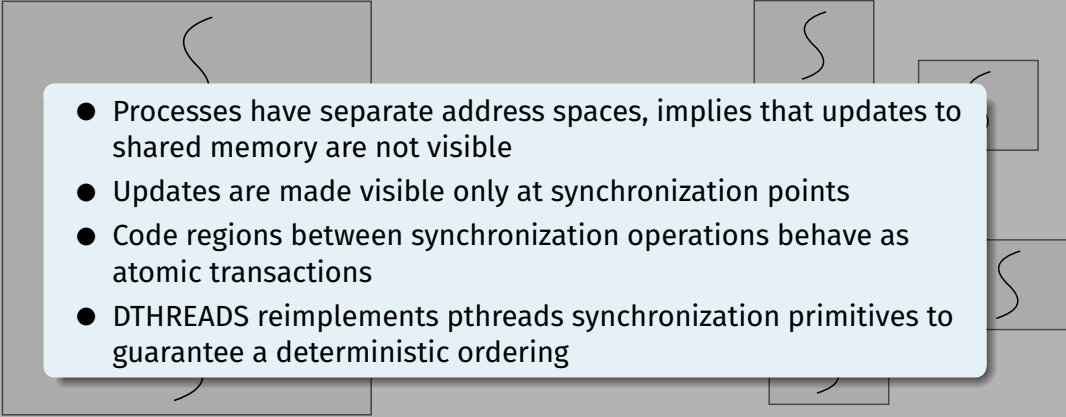
# Shared Address Space



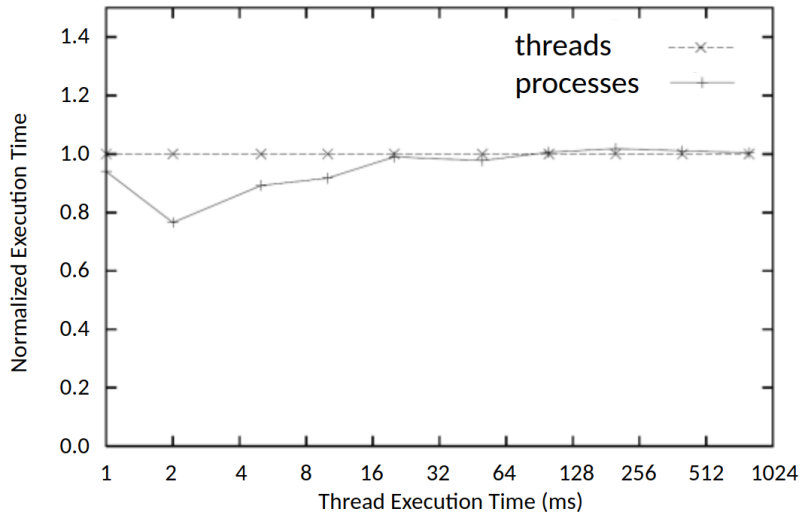
# Shared vs Disjoint Address Space



# Isolated Memory Access

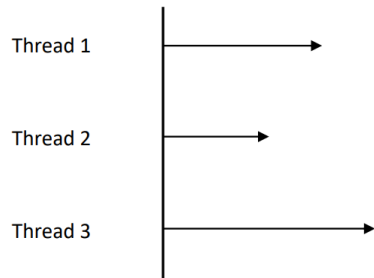
- 
- Processes have separate address spaces, implies that updates to shared memory are not visible
  - Updates are made visible only at synchronization points
  - Code regions between synchronization operations behave as atomic transactions
  - DTHREADS reimplements pthreads synchronization primitives to guarantee a deterministic ordering

# Performance of Threads vs Processes



# DTHREADS Phases

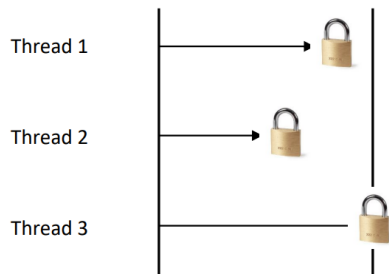
Parallel



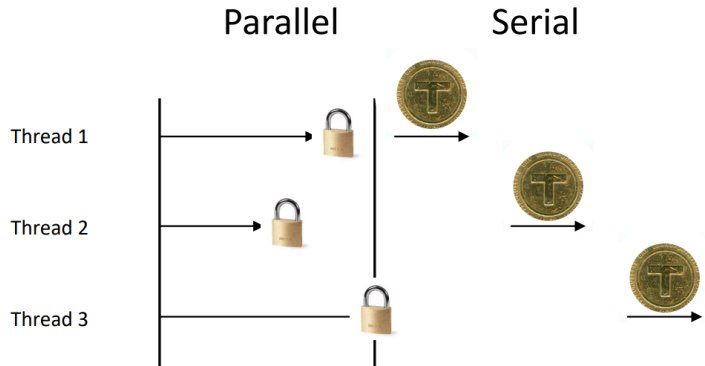


# DTHREADS Phases

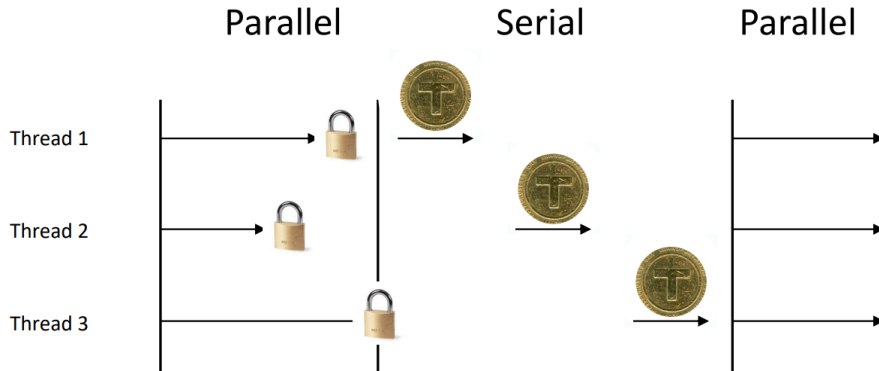
## Parallel



# DTHREADS Phases



# DTHREADS Phases



# Shared-Memory Updates in Parallel Phase

- DTHREADS uses memory-mapped files to share shared data (e.g., globals and heap) across processes
- Two copies of pages are created — one is read-only and the other is for local updates
- Threads have a read-only mapping of the shared pages at the beginning of the parallel phase
- Reads are performed from the shared page
- Upon a write, a private copy of the page is created (copy-on-write) and the write operates on the private copy

Snapshot pages before  
modifications



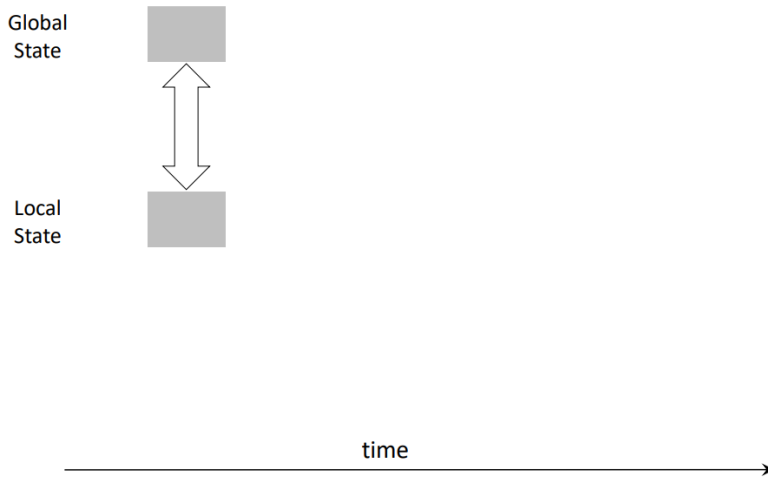
Snapshot pages before  
modifications



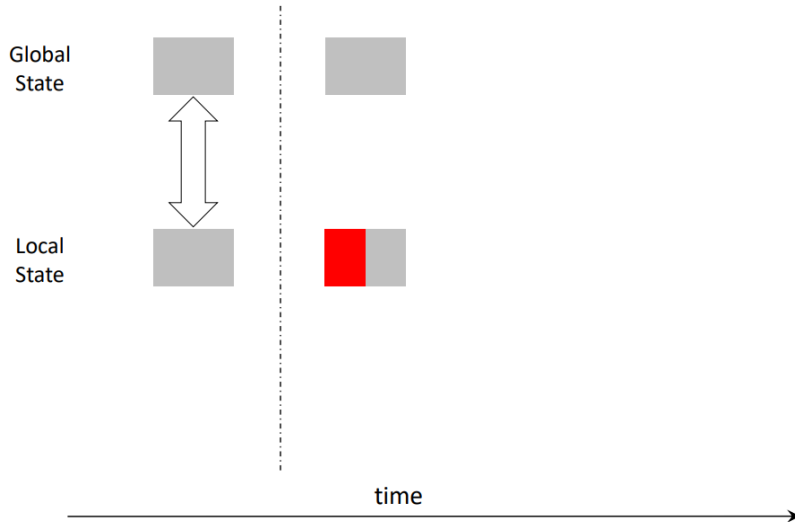
Write back diffs



# Commit Protocol

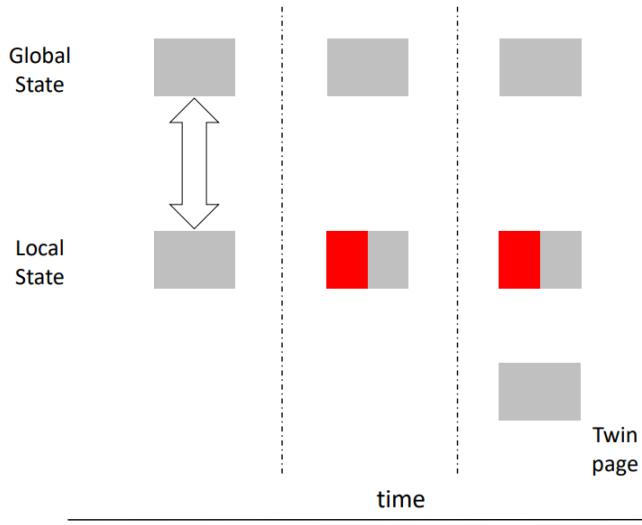


# Commit Protocol

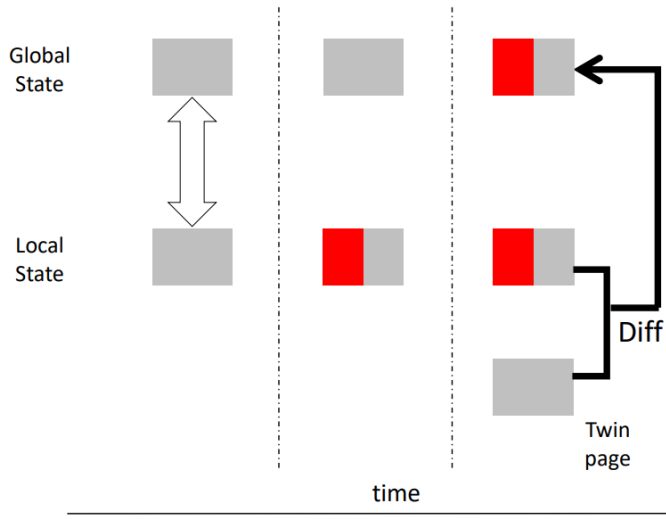




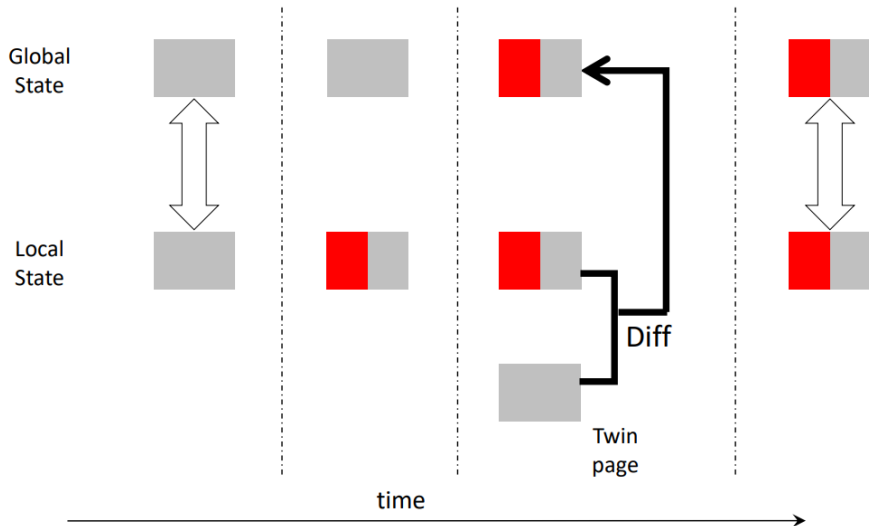
# Commit Protocol



# Commit Protocol



# Commit Protocol



# Commit Protocol

- During commit, DTHREADS compare the local copy with a “twin” copy of the original shared page
  - ▶ Writes back only the different bytes
  - ▶ First thread can copy back the whole page
- Private pages are released at the end of the serial phase

# DTHREADS Example Execution

a	0
b	0

Global State

```
if(a == 0)
    b = 1;
```

```
if(b == 0)
    a = 1;
```

# DTHREADS Example Execution

a	0
b	0

Global State

```
if(a == 0)
  b = 1;
```

a	0
b	0

a	0
b	0

```
if(b == 0)
  a = 1;
```

# DTHREADS Example Execution

a	0
b	0

Global State

```
if(a == 0)
  b = 1;
```

a	0
b	1

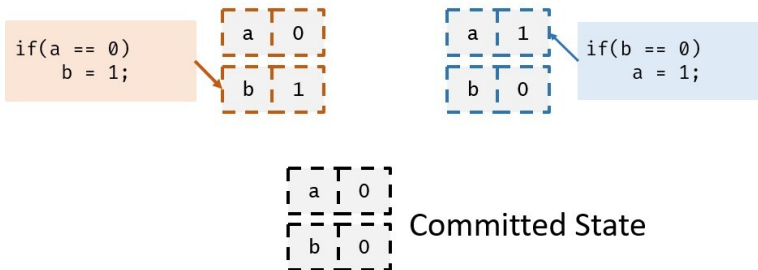
a	1
b	0

```
if(b == 0)
  a = 1;
```

# DTHREADS Example Execution

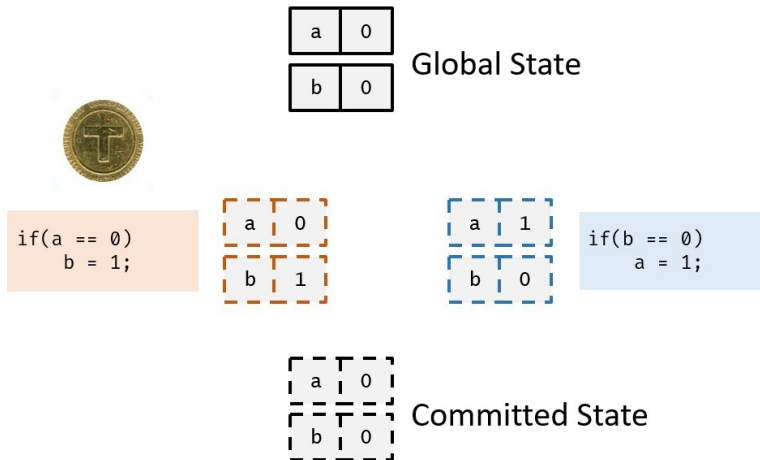
a	0
b	0

Global State

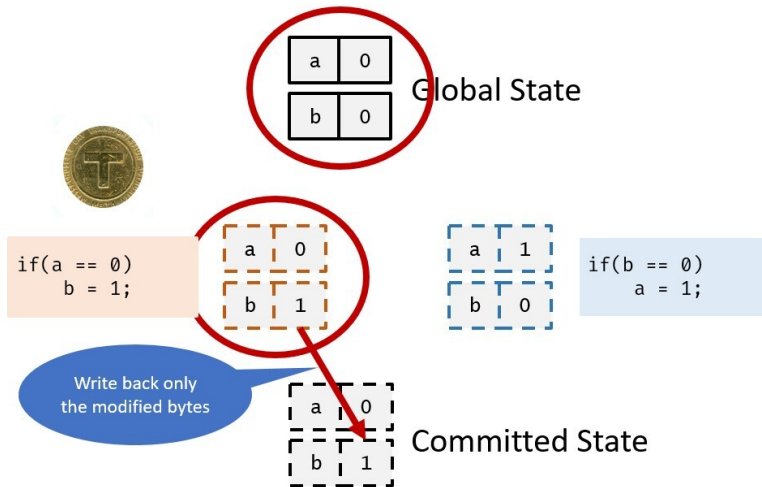




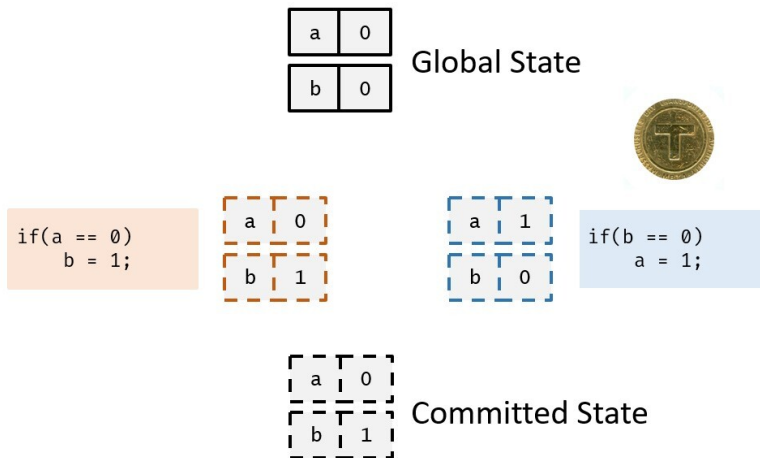
# DTHREADS Example Execution



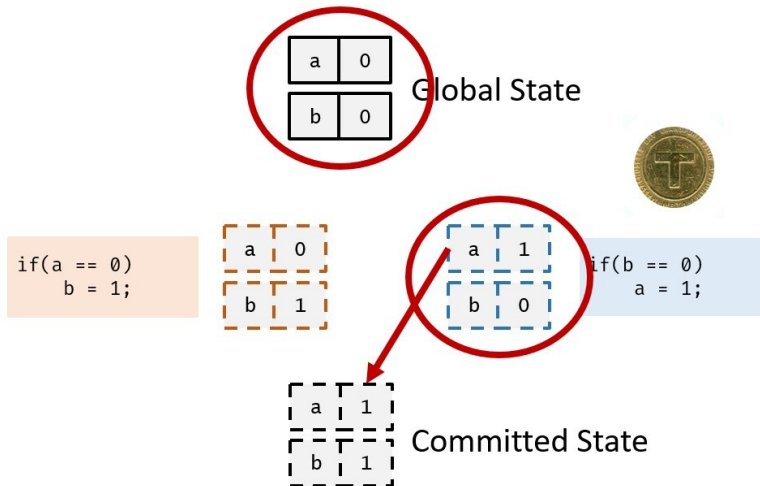
# DTHREADS Example Execution



# DTHREADS Example Execution



# DTHREADS Example Execution



# DTHREADS Example Execution

a	0
b	0

Global State

```
if(a == 0)
  b = 1;
```

a	0
b	1

a	1
b	0

```
if(b == 0)
  a = 1;
```

a	1
b	1

Committed State

# DTHREADS Example Execution

a	1
b	1

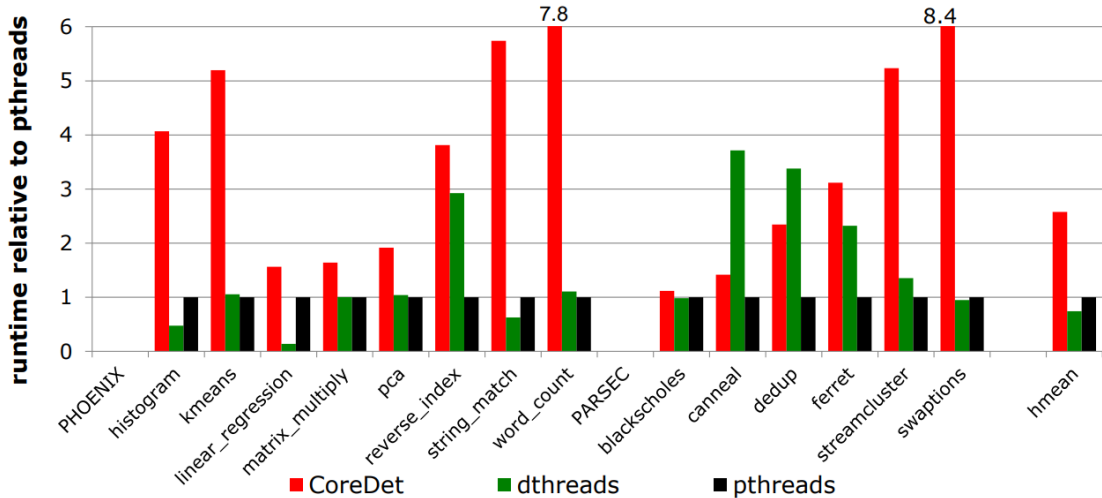
Global State

```
if(a == 0)
  b = 1;
```

a	0
---	---

b	0
---	---

```
if(b == 0)
  a = 1;
```



**Generally as fast or faster than pthreads**

# Fuzzing Concurrent Programs



# Fuzz Testing

Fuzzing is an automated software testing technique that is based on feeding the program with random inputs and monitoring the output

- Run the program with dynamic error detectors (e.g., Valgrind and AddressSanitizer)

**Advantages** + Easy to set up, can treat the application as a blackbox

**Disadvantages** — Probability of generating inputs that trigger an incorrect behavior is low if careful choices are not made  
— Inputs often require structure, random inputs are likely to be malformed

AFL<sup>†</sup>, AFL++<sup>§</sup>, and libFuzzer<sup>†</sup> are popularly used fuzzers

<sup>†</sup>american fuzzy lop

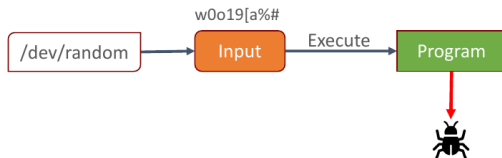
<sup>§</sup>American Fuzzy Lop plus plus (AFL++)

<sup>†</sup>libFuzzer — a library for coverage-guided fuzz testing



# Origin of Fuzz Testing

- On a night in 1988, Barton Miller tried to connect to his Unix system in office via a dial up connection
- There was heavy rain and thunderstorm which introduced disturbances (i.e., “fuzz”)
- Crashed many UNIX utilities he had been using successfully everyday
- He realized that there was something fundamentally wrong with the applications
- Asked three groups in his seminar course to implement this idea of fuzz testing
  - ▶ Two groups failed to achieve any crash results!
  - ▶ The third group succeeded!
  - ▶ Crashed 25-33% of the utility programs on the seven Unix variants that they tested



1990 study found crashes in:  
*adb, as, bc, cb, col, diction, emacs, eqn, ftp, indent, lex, look, m4, make, nroff, plot, prolog, ptx, refer!, spell, style, tsort, uniq, vgrind, vi*

# Types of Fuzz Testing

## Blackbox

- + Generates test cases based on the specification
- Ignores implementation details, may miss testing boundary cases
  - ▶ May rerun the same path over again (i.e., low coverage)
  - ▶ May be very hard to generate inputs for certain paths with restrictive conditions
  - ▶ May cause the program to terminate for logical reasons — fail format checks and stop

## Whitebox

- Fuzzing heuristics depend on the application internals to generate good test cases
- Tracks a coverage metric to estimate the quality of testing
- More smarter than blackbox, but complex and slower

## Graybox

- Fuzzing based on code coverage
- Instrument the program to track coverage

# Generating Inputs Randomly May Not be Effective



```
$ ant -f build.xml
```

```
<project default="dist">  
  <target name="init">  
    <mkdir dir="${build}"/>  
  </target>  
  ...
```

```
$ ant -f /dev/random
```

```
1rha3wn5p0w3uz;54 p0a23  
rw3i 50a20 5a2y58a2p  
y3wry3p285  
q@P"uer9zparu9apur9qa3802  
y5o2y 392r523a90wesu
```

# Generating Inputs Randomly May Not be Effective



```
$ ant -f build.xml
```

```
<project default="dist">
  <target name="init">
    <mkdir dir="${build}"/>
  </target>
  ...
</project>
```

```
$ ant -f /dev/random
```

```
1rha3wn5p0w3uz;54 p0a23
rw3i 50a20 5a2y58a2p
y3wry3p285
q@P"uer9zparu9apur9qa3802
y5o2y 392r523a90wesu
```

```
1 func(char *name, char *passwd, char *buf) {
2     if (authenticate_user(name, passwd)) {
3         if (check_format(buf)) {
4             update(buf); // crash here
5         }
6     }
7 }
```

# Mutation-based Fuzzing

- Take a well-formed input (i.e., seed) and randomly perturbs it (e.g., flip a bit) to generate new inputs
- Perturbation can use heuristics and domain knowledge
  - Binary input Flip bits or bytes and change random byte sequences
  - Text input Insert random symbols or keywords from a dictionary
- + Little or no knowledge of the structure of the inputs and the application is required
- Still prone to problems
  - ▶ Dependent on the quality of the initial test corpus
  - ▶ May rerun the same path over again
  - ▶ May be very hard to generate inputs for certain paths with restrictive conditions

# Generate Inputs Randomly via Mutation



\$ ant -f build.xml

```
<project default="dist">
  <target name="init">
    <mkdir dir="${build}"/>
  </target>
  ...
```

\$ ant -f build.xml.mut

```
<project default="dist">
  <taWget name="init">
    <maDir dir="2{build}"/@
  </tar?get>
  ...
```

# Mutation using Genetic Algorithms

- Mutational fuzzing can use genetic algorithms for generating mutations
- Genetic algorithms (GA) are search algorithms inspired from biology
  - ▶ Maintains a fixed-size population of possible solutions
  - ▶ Defines a set of mutation operators that combine solutions from the population to create new solutions
  - ▶ Applies the mutation operators to the current population to create a new “generation” of solutions
  - ▶ Uses a fitness function (e.g., code coverage) to prune the set of possible solutions to keep the most promising ones
  - ▶ Repeats until some stopping criteria is met



# Generational Fuzzing

- Test cases are generated from scratch
- Require some description of the input format: RFC and documentation
- Anomalies are added to each possible spot in the inputs
- + Knowledge of protocol should give better results than random fuzzing
- Requires a specification for every input format
- Writing test case generators is non-trivial

# Coverage-Guided Fuzzing

**Idea:** code that has not been covered by tests are likely to contain bugs

- Code coverage (e.g., line, branch, edge, or path) is used to determine how thoroughly code has been tested
- Steps in coverage-based fuzzing
  - ▶ Start with an initial user-provided test suite  $T$
  - ▶ Observe and track coverage while running tests from  $T$
  - ▶ Mutate test cases in  $T$  to generate new tests  $T'$
  - ▶ Run new tests from  $T'$
  - ▶ Move those tests that lead to new coverage from  $T'$  to  $T$
  - ▶ Continue fuzzing until the coverage goal is met
- Effectiveness of fuzzing is determined by the coverage of the program by the test suite
- Such an objective metric has many uses: stop testing, compare the quality of test suites, and generate test cases

# Graybox Fuzzing Workflow

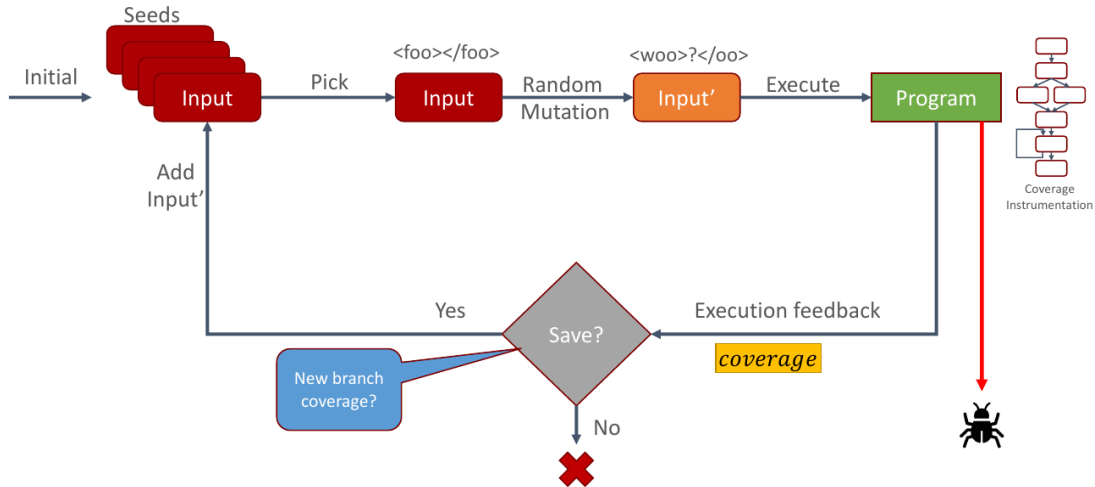
**Input** program  $P_o$ , initial seed queue  $Q_S$

**Output** final seed queue  $Q_S$ , vulnerable seed files  $T_C$

## Steps

```
 $P_f \leftarrow \text{instrument}(P_o)$  ▷ instrumentation  
 $T_C \leftarrow \Phi$   
while true do  
   $t \leftarrow \text{select\_next\_seed}(Q_S)$  ▷ seed selection  
   $M \leftarrow \text{get\_mutation\_chance}(P_f, t)$  ▷ seed scheduling  
  for  $i \in \{1, \dots, M\}$  do  
     $t' \leftarrow \text{mutated\_input}(t)$  ▷ seed mutation  
     $\text{res} \leftarrow \text{execute}(P_f, t', N_c)$  ▷ repeated execution  
    if  $\text{is\_interesting}(\text{res})$  then ▷ seed triaging  
       $T_C \leftarrow T_C \cup \{t'\}$  ▷ report  
    else if  $\text{new\_coverage}(t', \text{res})$  then  
       $Q_S \leftarrow Q_S \oplus t'$  ▷ preserve effective seeds
```

# Coverage-Guided Fuzzing



# Coverage-Guided Fuzzing with AFL

- One of the first popular coverage-guided fuzzers
  - ▶ Started by Michal Zalewski (lcamtuf)
- AFL instruments branch statements and tracks code paths taken at run time
- AFL is very easy to use and has been very effective
  - ▶ Provides a GCC wrapper to instrument the code
  - ▶ Uses counters to track edges in the control flow graph
  - ▶ Uses hashing to encode different edges (imprecise but efficient)



american fuzzy lop 0.47b (readpng)			
<b>process timing</b>		<b>overall results</b>	
run time : 0 days, 0 hrs, 4 min, 43 sec		cycles done : 0	
last new path : 0 days, 0 hrs, 0 min, 26 sec		total paths : 195	
last uniq crash : none seen yet		uniq crashes : 0	
last uniq hang : 0 days, 0 hrs, 1 min, 51 sec		uniq hangs : 1	
<b>cycle progress</b>		<b>map coverage</b>	
now processing : 38 (19.49%)		map density : 1217 (7.43%)	
paths timed out : 0 (0.00%)		count coverage : 2.55 bits/tuple	
<b>stage progress</b>		<b>findings in depth</b>	
now trying : interest 32/8		favored paths : 128 (65.64%)	
stage execs : 0/9990 (0.00%)		new edges on : 85 (43.59%)	
total execs : 654k		total crashes : 0 (0 unique)	
exec speed : 2306/sec		total hangs : 1 (1 unique)	
<b>fuzzing strategy yields</b>		<b>path geometry</b>	
bit flips : 88/14.4k, 6/14.4k, 6/14.4k		levels : 3	
byte flips : 0/1804, 0/1786, 1/1750		pending : 178	
arithmetics : 31/126k, 3/45.6k, 1/17.8k		pend fav : 114	
known ints : 1/15.8k, 4/65.8k, 6/78.2k		imported : 0	
havoc : 34/254k, 0/0		variable : 0	
trim : 2876 B/931 (61.45% gain)		latent : 0	

# Comparing Fuzzing Approaches

- Graybox fuzzing (e.g., AFL, libFuzzer, and Honggfuzz)
  - + Requires minimal setup similar to blackbox fuzzing
  - + More targeted than blackbox fuzzing, but does not understand the program
  - Searches for inputs independently from the program
  - May not be able to execute some code paths
- Whitebox fuzzing
  - ▶ Couples test case generation with fuzzing
  - ▶ Test generation is based on static analysis and/or symbolic execution
    - Run the code with some initial input
    - Collect constraints on input with symbolic execution
    - Generate new constraints
    - Solve constraints with constraint solver
    - Synthesize new inputs
  - ▶ Rather than generating new inputs and checking whether they cover a new path, compute inputs that **will execute a desired** path

# Challenges with Fuzzing

- Mutation heuristics
  - ▶ Which inputs to mutate? How many times? How to generate meaningful test cases?
- Coverage
  - ▶ What to instrument to improve feedback? How to keep overhead low?
- Oracle
  - ▶ How to monitor the application to find a bug?
    - For example, a crash or silent overflow or infinite loop or race conditions?
  - ▶ Instrument the program with runtime sanitizers to monitor abnormal program execution
  - ▶ Use Valgrind or sanitizers<sup>†</sup> (e.g., ASAN, TSAN, and UBSAN)
- When do we stop fuzzing?
  - ▶ Need to balance cost vs bug coverage

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<sup>†</sup><https://github.com/google/sanitizers>

# Power Schedules with Mutational Fuzzing

- Consider a new generation of test inputs containing
  - ▶  $n - 1$  inputs that have been in the population for at least a few generations,
  - ▶ one input that covered a new branch or path that was created in the last round of mutation
- Which input should we mutate?
  - ▶ Intuitively, we expect that the new input should be mutated more often in the next generation
  - ▶ This intuition is implemented via power schedules



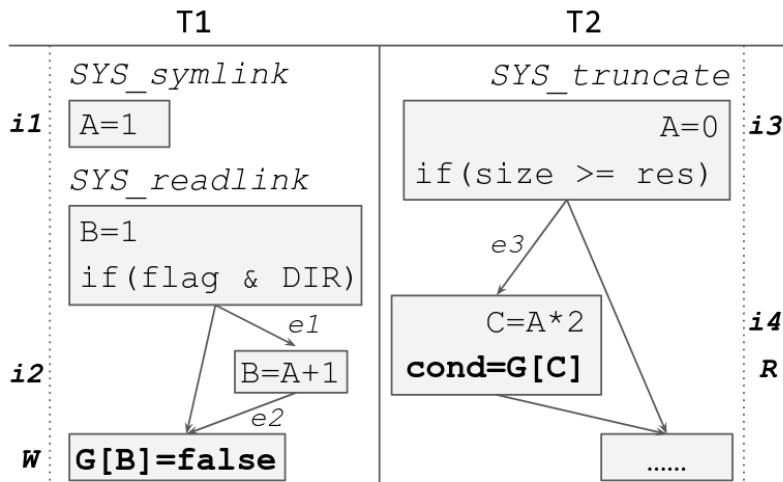
# Power Schedules with Mutational Fuzzing

- A power schedule distributes fuzzing time among the seeds in the population
- Each seed is assigned an energy value using a policy
  - ▶ Seeds that exercise rarely-covered paths have more energy
  - ▶ Seeds that exercise code close to the area of interest (e.g., modifications) is given more energy (called directed fuzzing)
- The chances of mutating a seed are proportional to its energy
- Usual policy is:
  - ▶ Newly-discovered seeds start with high energy
  - ▶ When a seed is mutated to produce an input that increases fitness, its energy increases
  - ▶ When a seed is mutated but does not produce an input that increases fitness, its energy decreases

# Fuzzing Concurrent Programs

- Goal is to use fuzzing to detect concurrency bugs like data races and deadlocks
  - (i) Explore as many code paths and thread interleavings as possible
  - (ii) Use a “good” bug detection algorithm
- How about reusing existing pipelines meant for sequential programs?
  - ▶ For example, AFL+TSAN or Syzkaller+KCSAN for data races
- Existing fuzzers use coverage meant for sequential programs (e.g., branch coverage)
- Do not effectively prioritize exploring thread interleavings

# Limitations with Branch Coverage



# Limitations with Branch Coverage

T1	T2	T1	T2	T1	T2
A=1		A=1		A=1	
B=A+1			A=0		A=0
	A=0	B=A+1			C=A*2
	C=A*2		C=A*2	B=A+1	
① B=2, C=0	<nil>	② B=1, C=0	i3→i2	③ B=1, C=0	i3→i2
T1	T2	T1	T2	T1	T2
	A=0		A=0		A=0
	C=A*2	A=1		A=1	
A=1			C=A*2	B=A+1	
B=A+1		B=A+1			C=A*2
④ B=2, C=0	<nil>	⑤ B=2, C=2	i1→i4	⑥ B=2, C=2	i1→i4

# Concurrency Coverage

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- Check for bugs among possibly overlapping concurrent instructions from different threads
- Alias instruction pair describes the locations of two concurrently-executed instructions
- Alias coverage tracks how many such interleaving points have been covered during testing

# Data Race from JFS (Linux kernel v5.4)

## Thread 1

File: linux/fs/jfs/jfs\_txnmgr.c

```
1 void txEnd(...) {  
2     ...  
3     // racy read  
4     log = JFS_SBI(tblk->sb)->log;  
5     ...  
6     if (--log->active == 0)  
7     ...  
8 }
```

## Thread 2

File: linux/fs/jfs/jfs\_logmgr.c

```
1 int lmLogClose(...) {  
2     ...  
3     struct jfs_sb_info *sbi = JFS_SBI(sb);  
4     ...  
5     // racy write  
6     sbi->log = NULL;  
7     ...  
8 }
```

The data race was introduced in Linux kernel 2.6.12 in June 2005 and was hidden for fifteen years

# Importance of Context-Sensitive Call Pairs

## Call Pair 1

```
Thread 1  jfs_lazycommit() -> txLazyCommit() -> txEnd()  
Thread 2  jfs_put_super() -> jfs_umount() -> lmLogClose()
```



## Call Pair 2

```
Thread 1  jfs_lazycommit() -> txLazyCommit() -> txEnd()  
Thread 2  jfs_remount() -> jfs_umount() -> lmLogClose()
```



# Context-Sensitive Concurrency Coverage

Maintain information of a function call (*CallInfo*) as a tuple of the call site (*CallLoc*) and the location of the function definition (*FuncLoc*)

$$CallInfo = [CallLoc, FuncLoc]$$

Maintain the calling context (*CallCtx*) as the list of function calls in the run-time call stack

$$CallCtx = [CallInfo_1, CallInfo_2]$$

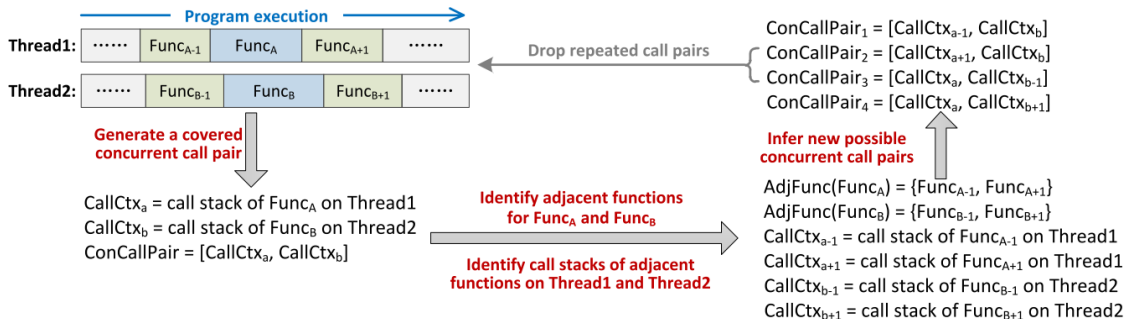
Concurrent call pair maintains the calling contexts of concurrently executing functions

$$ConcCallPair = \{CallCtx_1, CallCtx_2\}$$



# Adjacency-Directed Mutation

If two functions are concurrently executed, the adjacent functions in their call stacks can probably be executed concurrently as well



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