# Trajectory (Motion) Estimation Of Autonomously Guided Vehicle Using Visual Odometry 

By

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#### Abstract

Visual odometry is a technique to determine coordinates of a vehicle or any object by using surrounding visual information. The approach is revolutionary for small autonomously guided vehicles. Because in indoors performance is very poor. And IMUs at small scale are very sensitive to noise. And IMUs can also give unexpected results which may lead to erroneous motion estimation. Technique utilizes some state of the art techniques like feature detection, tracking and some mathematics of camera theory.


## I. INTRODUCTION

Odometry is a process of estimating motion parameters using various kinds of sensors like IMUs, GPS. When we do this using visual information (Images), it is called visual odometry. The term Visual Odometry was first used by David D. Nister in 2004[1]. Which was named so because it is similar to Wheel odometry, in which we integrate the angle of the wheels over time. In Visual Odometry we integrate images over time. Problem with wheel odomtery is "wheel slip". Which if not incorporated in the estimation, can lead to highly erroneous results.

Visual odometry was first used in NASA's Mars rover "Phoenix" and "Opportunity". And today a lot of research is going on in this field.

So precisely in this particular application of visual odometry, we estimate trajectory covered by autonoumous ground vehicles (UGV-unmanned ground vehicles)[1]. we'll be given some images captured from camera mounted on the UGV and I need to preccess them through visual odometry system. Visual odometry system involves a various step process which in turn includes feature detection, feature matching or tracking, RANSAC, motion estimation and offline adjustment. Odometry can be done by a
monocular camera or stereo camera. Stereo camera often provides better results due to less reconstruction errors involved in estimating motion.

## II. A BRIEF INTRODUCTION TO WHAT I HAVE DONE

I Downloaded data set of 443 images from Karlsruhe Institute of technology, Chicago, which is technological institute of TOYOTA in area of autonomous vehicles research[6].

I went through the maths of the system given in [1],[2],[3],[4],[5].Actually there is a lot of maths involved in this project but it is quite interesting. The maths is from two different parts. One from images processing and another from camera theory. Combining these two gives birth to this beautiful project.

Then I wrote the whole program in MATLAB to test the algorithm. Used Some inbuilt functions of MATLAB like feature detection, matching, because these are highly optimized function.

After this I wrote the whole code in Visual basic .NET for real time implementation using EmguCV (.NET wrapper of OpenCV )[7]. Then I Interfaced MATLAB with Visual basic to plot trajectory graphs.

I have also implemented code using feature matching and feature tracking. The later is giving very good results.

## III. PROBLEM FORMULATION

Aim: To estimate camera poses from set of images taken at discrete interval
Indirectly: We have to find a Transormation matrix which relates two image frames i.e. how the two frames are rotated and translated from each other.

Reffering to [1], let a set of images be $\left\{I_{0}, I_{1}, I_{2} \ldots I_{k-1} I_{k}\right\} \quad$,camera poses be $\left\{C_{0}, C_{1}, C_{2} \ldots C_{k-1}, C_{k}\right\}$ and transformation matrix is given by

$$
T_{k, k-1}=\left[\begin{array}{cc}
R_{k, k-1} & t_{k, k-1}  \tag{1}\\
0 & 1
\end{array}\right]
$$

here $T_{k, k-1}$ is homogenous transformation matrix between images $I_{k}$ and $I_{k-1} . R_{k, k-1}$, $t_{k, k-1}$ are rotation and translation matrix between images $I_{k}$ and $I_{k-1}$.


Fig 1. Image Courtesy: "Learning OpenCV, O'REILLY"
In the above figure, take $O_{l}, O_{r}$ as position of camera at time $t_{1}, t_{2}$, which can be reffered as image_1 and image_2. As you can see image_1 has been translated by a translation vector of ' T ' and rotated by rotational matrix 'R'.
' $R$ ' is a matrix of $3 \times 3$, ' $T$ ' is $3 \times 1$ vector which represents translation in $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ direction respectively and $T_{k, k-1} 4 \times 4$ matrix to combine the effect of R and T .

The camera pose at time $t_{k}$ is given by

$$
\begin{equation*}
C_{k}=T_{k, k-1} * C_{k-1} \tag{2}
\end{equation*}
$$

 30 Years and Fundamentals"

Fig 2 shows poses of a stereo camera at different time instants. $C_{k-1}$ and $C_{k}$ are camera poses at time instants $t_{k-1}, t_{k}$ respectively. For more information on transformation refer to chapter 2 of [4].

Let us suppose vehicle started $(0,0,0)$ of real world coordinate, then position of vehicle at time $t_{k}$ is given by last column of matrix $T_{k, k-1}$ whose last element is 1 .

## IV. PREREQUISITES

- Camera Theory.
- Strong Knowledge of Camera intrinsic and extrinsic parameters.
- Spatial Transformation
- Image Basics
- Image Features

Above are some topics which are required you to gone through, because these terms will be used frequently in subsequent explanations.

For camera theory you can refer to [4], which is known as Bible of camera theory. And for Spatial transormations chapter 2 of [8] is enough.

Image Basics involves some basic knowledge and working with multidimensional matrices and RGB, Gray scale images. For this a lot of online tutorials are available.

For image features also, you can find best tutorials on internet. But the feature I have used will be described in a bit lesser detail.

As we move on I'll keep on introducing new things and their details.


Fig3 Algorithm

## a. Feature detection

A feature in an image nothing but only a point a interest. We apply mathematical operations on those points only rather whole image.

A lot of feature detection algorithms are available. We can choose any of them but for this particular application I have tested SIFT, FAST, FREAK, Harris, SURF, Shi-Tomasi.

Motion estimation using SIFT, SURF, FREAK takes a lot of computational time. Where as Shi-Tomasi corners are computed in lesser time and for motion estimation these doesn't eat much time.

I used SIFT,SURF, FREAK for feature matching and Shi-Tomasi, Harris for feature tracking.

Feature tracking provided very good results then feature matching with drastic improve in computation time.

## Functions used (Objects in language) :

MATLAB:

1. detectSIFTFeatures
2. detectSURFFeatures
3. detectFASTFeatures

OpenCV:

1. SIFTDetector
2. SURFDetector
3. GFTTDetector

For more refer to documentation of EmguCV [7].
b. (i) Feature Matching

Suppose you have detected features 50 and 60 features in two consecutive images im1 and im 2 respectively. Feature matching means finding an approximate match of 50 features in im 1 to 60 features in im2.

Precisely we want to know where these 50 features of image-1 are in image-2 (Camera1 ,Camera-3). These matches are called correspondents. The matches can be found using radial match or k -nearest neighbor match. I have used K-NN.

In K-NN we find distance of each of 50 features of image- 1 from 60 feature of image- 2 . Then we only retain the points (matches) which are having distance between then below a threshold. Threshold is set heuristically.

For feature matching we need additional functions.But these are not required in feature tracking.
Functions used (Objects in language) :
MATLAB:

1. extractFeatures
2. matchFeatures

## OpenCV:

1. ComputeDescriptorsRaw
2. knnMatch (FLANN class OpenCV)

## b. (ii) Feature Tracking

Difference between feature matching and feature tracking is as follows. Feature matching means independently finding features in two frames and matching them. Whereas feature tracking means finding features in one image only and tracking them in subsequent images[2]. It may happen that some feature may get lost due to occlusion or out of field of view of camera. So you have to add some new best strong points. I have used feature tracking only in OpenCV due to time constraint.

For tracking first we detect best feature called Shi-Tomasi features or GoodFeaturesToTrack[10] and then use sparse version of Kannade-Lucas-Tomasi tracker using optical flow. For KLT refer to the original implementation [9].
Functions used (Objects in language) :
OpenCV:

1. GFTTDetector
2. cvCalcOpticalFlowPyrLK

## c. Outlier Removal using RANSAC

From feature matching (tracking depending what you have used), we have obtained point correspondences (matches). Some of the matches even after thresholding may be wrong. The wrong matches are called 'Outliers' and correct ones are called 'Inliers'.

The outliers can greatly diminish performance of Visual Odometry system. So before motion estimation we have to remove these outliers. Popular method is to use RANSAC (Random Sampling And Consenous).

As reffered by [1], In brief RANSAC works like this. Take any two correspondents from the matches and fit a line between them. Compute distance of remaining point from this line. Save the points which are having distance below a threshod. These are inliers. Keep on repeating this method to obtain as many inliers as you want.

RANSAC is a non-determinstic technique to obtain inliers. No of loops required is given by $N=\frac{\log (1-p)}{\log \left(1-(1-\varepsilon)^{s}\right)}$
$\mathrm{p}=$ probability of success
$\varepsilon=\%$ of outliers in data
$\mathrm{s}=$ no of points by which model can be instantiated


Fig4. Image Courtesy: DavideScaramuzza @ieee.org

So after RANSAC we only have inliers.


Fig 5. Snapshot of my application in .NET showing outliers


Fig 6. Outliers removed using RANSAC
Let Point correspondents are denoted by $x, x^{\prime}$ in $1^{\text {st }}$ and $2^{\text {nd }}$ image respectively. $x, x^{\prime}$ are 3 x 1 homogenous vector i.e. $3^{\text {rd }}$ element is equal to 1 .

## d. Motion Estimation

Before we proceed to motion estimation, it is required to get familiar with some of camera concepts like its intrinsic and extrinsic parameters. For Maths involved in Motion
estimation we'll refer to [4]. Most of maths is from Part II of [4].

Intrinsic Parameters of camera is the calibration matrix of camera which give you the perspective projection. It is a $3 \times 3$ matrix denoted by ' K '.

$$
K=\left[\begin{array}{ccc}
\alpha_{u} & 0 & u_{0}  \tag{4}\\
0 & \alpha_{v} & v_{0} \\
0 & 0 & 1
\end{array}\right]
$$

$\alpha_{u}, \alpha_{v}$ are the scale factor in $\mathrm{x}, \mathrm{y}$ direction due to perspective projection. $u_{0}, v_{0}$ are center of image.

Next I'll describe about various frames of references i.e. world coordinate frame,


Fig7. Image Courtesy: "Visual Odometry: Part I - The First 30 Years and Fundamentals"

The Image Frame may be rotated w.r.t. world coordinate system (C) .let the rotation be ' $R$ ' and translation be ' $t$ '. then a matrix $\mathrm{P}=[\mathrm{R} \mid \mathrm{t}]$ is called extrinsic parameters matrix. So let ' $x$ ' be a point in image plane w.r.t frame of ref (I) and ' X ' be a point w.r.t. world coordinate system then

$$
\begin{equation*}
x=K P X \tag{5}
\end{equation*}
$$

$x$ is $3 \times 1$ homogenous vector. K is $3 \times 3$ calibration matrix. P is $3 \times 4$ matrix and $X$ is $4 \times 1$ homogenous vector.

So from here you can understand that we have to estimate ' $R$ ' and ' $t$ ' w.r.t. a frame of reference given by

$$
\mathrm{P}=\left[\begin{array}{llll}
1 & 0 & 0 & 0  \tag{6}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0
\end{array}\right]
$$

Refer to [4] for more detail on this.

## (i) Estimating ' $R$ 'and ' $t$ '

There is something called essential matrix which is combination of ' $R$ ' and ' $t$ '. and is given by

$$
E=\left[\begin{array}{ccc}
0 & -t_{z} & t_{y}  \tag{7}\\
t_{z} & 0 & -t_{x} \\
-t_{y} & t_{x} & 0
\end{array}\right]\left[\begin{array}{l} 
\\
R_{k, k-1}
\end{array}\right]
$$

So now you may have understood the point that we have to estimate this essential matrix and then break into ' $R$ ' and ' $t$ '.

To estimate ' $E$ ' matrix we have a lot of algorithms available. For example Normalized 8 point algorithm, 7 point algorithm, Nister's 5 point algorithm, RANSAC-1 point algorithm.

A condition of epipolar geometry is satisfied by this ' $E$ ' matrix. Which is called epipolar constraint and is given by

$$
\begin{equation*}
x^{\prime T} E x=0 \tag{8}
\end{equation*}
$$

From RANSAC output we have $x, x^{\prime}$. We put $x, x^{\prime}$ in above equation and estimate E . You might be thinking that I have points to solve the equation, then why I am saying that "we are esitimating ' $E$ '"? This is because RANSAC output is non deterministic. So we have only an estimate of correct correspondences.

I have used Normalized 8 point algorithm.
Functions used (Objects in language):

## MATLAB:

1. estimateFundamentalMatrix

OpenCV
2. cvFindFundamentalMat

Lets imagine that first camera pose is denoted by P and second by P '. Where ' P ' is of the form given by (6) and $P$ ' $=[R \mid t]$. where ' $R$ ' and ' $t$ ' are are rotation and translation vector by which camera-2 has been transformed w.r.t. camera-1.

Aim is to estimate ' $R$ ' and ' $t$ ' from ' $E$ ' matrix. So for this we take SVD of 'E' matrix. There is special method to take SVD of essential matrix. For which you can refer to appendix B refer to [3].

As given in [1], Let SVD of ' $E$ ' matrix is given by $U D V^{T}$ and a matrix ' W ' is given by then we get four solutions given by

$$
W^{T}=\left[\begin{array}{ccc}
0 & \pm 1 & 0  \tag{9}\\
\mp 1 & 0 & 0 \\
0 & 0 & 0
\end{array}\right]
$$

$$
\begin{gather*}
R=U\left( \pm W^{T}\right) V^{T} \\
t= \pm\left[u_{13}, u_{23}, u_{33}\right] \tag{10}
\end{gather*}
$$

Out of these four solutions only one corresponds to true configuration. And these four solutions corresponds to configurations in space as given below


Fig 8. Image Courtesy: "Hartley, Zisserman - Multiple View Geometry in Computer Vision"

Now we have to select only one correct configuration out of these four. To do this we use a variant of direct linear transform as given in chapter 12 of [4] on page no 312 .

DLT is used to triangulate a point. Means finding $\mathrm{x}, \mathrm{y}, \mathrm{z}$ of an image point in world coordinate system. After triangulation we put a constraint on the triangulated point that it must be in front of both of the cameras. This is chiral constraint given in [3].

Since this constraint will be fulfilled by only one configuration, so now we have ' $R$ ' and ' $t$ ' which relates camera- 1 and camera-2. The process is repeated for subsequent images and at any time we can tell $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ coordinate of the vehicle w.r.t. the point from it started.

Now we concatenate all the $T_{k, k-1}$ matrices to obtain position on $N^{t h}$ frame w.r.t. the point from where the vehicle started. So position of $N^{\text {th }}$ frame is w.r.t. to starting point is given by

$$
\begin{gather*}
{ }_{N}^{0} T={ }_{1}^{0} T{ }_{2}^{1} T{ }_{3}^{2} T \ldots \ldots .{ }_{N}^{N-1} T  \tag{11}\\
{ }_{N-1}^{N-1} T={ }_{N-1}^{N} T^{-1}
\end{gather*}
$$

So let us take starting point be $(0,0,0)$. And ' $R$ ' and ' $t$ ' be the correct configuration of camera-2 w.r.t. camera-1 . Then location of camera-2 w.r.t. is given by

$$
X=[R \mid t]^{-1}[0,0,0,1]^{T}
$$

' $X$ ' is ( $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ ) of camera-2 w.r.t frame of reference of camera-1

## b. Optional Bundle Adjustment

As name suggests it is optional to use. Although I havn't used it but I'll explain in short what it is. For more details on it please refer to [2].

Bundle means set of transformation matrices. We take previous ' $m$ ' transformation matrix to find next transformation matrix. This eliminates disparity problem if frames are too close.

As described in [2] ,In fig 9 uncertainity of pose $C_{k}$ is combination o uncertainity in $C_{k-1}$ and $T_{k, k-1}$.


Fig 9. Image Courtesy: Visual Odometry: Part II - Matching, Robustness, and Applications

And we are done. Now its time to have a look on my program's results. I used DATA SET from KITTI [7], Karlsruhe Institute of technology, Chicago. Which has color as well as grayscale images in separate folders. They also have provided ground truth data( IMU data, GPS data), calibration matrix. Ground truth is used to compare results. I'll Show my results both using feature matching and feature tracking.

## Results

Car Used In Capturing Images


Fig 10. Image Courtesy: "The KITTI Vision Benchmark suite"
From fig 10 you can see that according to camera (Red) forward direction is ' $Z$ ' axis, left is ' X ' and ' Y ' is pointing downwards. And for $\operatorname{IMU}($ Green ) ' X ' is pointing forward, Y ' is


Fig 11. Image Courtesy: "The KITTI Vision Benchmark suite"
leftward and ' $Z$ ' is pointing upward. So according to ground truth ' X ' compnents will be the direction of motion.

Some SnapShots of my .NET application


Fig 12. Feature matching Technique using FAST detection and SURF extraction on DATA SET images


Fig 13. Feature Tracking Technique using Shi-Tomasi features detection and Sparse version of Kannade-Lucas-Tomasi Tracking on DATA SET images


Fig 14. Feature Tracking Technique using Shi-Tomasi features detection and Sparse version of Kannade-Lucas-Tomasi Tracking on DATA SET images


Fig 15. Feature Tracking Technique using Shi-Tomasi features detection and Sparse version of Kannade-Lucas-Tomasi Tracking on Live camera

## Ground truth



Fig 16 Ground Truth provided by IMU and GPS mounted on the Car

Ax, Vx - Acceleration, velocity in x direction.
$\mathrm{Ay}, \mathrm{Vy}$ - Acceleration, velocity in y direction.
$\mathrm{Az}, \mathrm{Vz}$ - Acceleration, velocity in z direction.
X - X coordinate of Vehicle
Y - Y coordinate of Vehicle
Z $\quad$ Z coordinate of Vehicle


Fig17 Results of OpenCV using feature matching


Results of MATLAB using feature matching


Ground Truth


Fig18 Results of OpenCV using feature tracker

Difference between the results of OpenCV for matching and tracking is the part where car stops for a couple of seconds. In feature matching, I was getting a non-zero translation even the car was stopped. But Using feature tracking I got a nearly zero translation when car was stopped. You can notice the difference in The results of OpenCV by the arrow tip. In feature matching results, you can see some pixels outside of trajectory. Those are wrong results. But in Feature tracking this is removed.

## Data Set

1. Karlsruhe institute of Technology, Chicago (Technogical research institute of TOYOTA for Autonoumous vehicles)
2. Raw 443 unrectified gray scale images of size $1392 \times 512$ of .png format.3. Images are captured in City.

## Softwares Used

1. MATLAB 2013, MathWorks.
2. Visual Studio 2013 Express Edition for Visual Basic.
3. EmguCV, a .NET wrapper of OpenCV Binaries.

## References:

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