# Potential Field Guided Sampling Based Obstacle Avoidance 

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## Introduction to the Problem

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Given a source $S$, a destination $D$ and an obstacle space $Q$ we need to compute a smooth path from $S$ to $D$ avoiding $Q$.

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In our model, we will represent this path as a sequence of nodes $S$, $X_{1}, X_{2}, X_{3}, \ldots, X_{n}, D$ such that there is an edge connecting every pair of consecutive nodes and none of these edges collide with the obstacle space $Q$.

## Previous Work

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- Probabilistic Roadmap (PRM)


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- Artificial Potential Field (APF)


## Probabilistic Roadmap

## Probabilistic Roadmap

- Takes random samples from the configuration space of the robot
- Use a local planner to connect these configurations to other nearby configurations
- Insert the starting and goal configurations
- Use any shortest path graph algorithm to determine a path from source to destination


## Rapidly Exploring Random Tree

## Rapidly Exploring Random Tree

- Grows a tree rooted at the start configuration using random samples
- Creates an edge between the sample and the nearest tree node
- Adds the randomly generated node to the tree
- RRT growth can be biased by increasing the probability of sampling states from a specific area
- The sampling is stopped whenever a sample is generated in the goal region


## Rapidly Exploring Random Tree Star

## Rapidly Exploring Random Tree Star

- Optimised version of RRT
- Minimises the distance from the root to the tree nodes at each iteration


## Artificial Potential Field

## Artificial Potential Field

- Finds an artificial potential in the configuration space
- Negative gradient of this potential is the force
- Robot moves in small incremental steps in the direction given by that of the net force
- Robot always follows minimum potential path from the source to the destination


## Drawbacks

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RRT* generates a path which is approximately optimal from the source to the destination but the path returned by this algorithm has sharp corners which are practically difficult to negotiate. The convergence to the optimal solution takes infinite time.

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APF generates a smooth path from the source to the destination but leaves the robot stranded at points of local minima.

## Our Approach

- Unify the RRT* algorithm with the APF algorithm into a Potential Guided Directional-RRT* algorithm
- Enhance the rate of convergence towards the optimal solution
- A smooth path from the source to the destination


## Our Approach

- Generate a random sample
- Apply the potential field model to generate a new point by moving a small incremental distance in the direction of net force
- Carry out the RRT* algorithm treating this new point as the randomly generated point


## References

- A.H. Qureshi, K. F. Iqbal, S. M. Qamar, F. Islam, Y. Ayaz and N. Muhammad: Potential Guided Directional-RRT* for Accelerated Motion Planning in Cluttered Environments
- S. Karaman and E. Frazzoli: Sampling-based Algorithms for Optimal Motion Planning
- J. Nasir, F. Islam, U. Malik, Y. Ayaz, O. Hasan, M. Khan and M. S. Muhammad: RRT*-Smart: A Rapid Convergence Implementation of RRT*
- S. Byrne, W. Naeem and R. S. Ferguson: Efficient Local Sampling for Motion Planning of a Robotic Manipulator


## RRT Pseudo Code

```
RRT ()
V\leftarrow{\mp@subsup{x}{\mathrm{ init }}{}}
E}\leftarrow
for i=1,2,\ldots,n do
    x rand }\leftarrow\mp@subsup{\mathrm{ SampleFree }}{i}{
    x nearest }\leftarrow\operatorname{Nearest (G, xrand}
    x new }\leftarrow\operatorname{Steer}(\mp@subsup{x}{\mathrm{ nearest }}{},\mp@subsup{x}{\mathrm{ rand }}{}
    if ObstacleFree( }\mp@subsup{x}{\mathrm{ nearest }}{},\mp@subsup{x}{\mathrm{ new }}{})\mathrm{ then
    V\leftarrowV\cup{\mp@subsup{x}{new}{*}}
    E\leftarrowE\cup{(\mp@subsup{x}{\mathrm{ nearest }}{},\mp@subsup{x}{\mathrm{ new }}{})}
return G = (V,E)
```


## RRT* Pseudo Code

```
RRT* ()
\(V \leftarrow\left\{x_{\text {init }}\right\} ; \quad E \leftarrow \phi\)
for \(i=1,2, \ldots, n\) do
    \(x_{\text {rand }} \leftarrow\) SampleFree \(_{i} ; \quad x_{\text {nearest }} \leftarrow \operatorname{Nearest}\left(G, x_{\text {rand }}\right)\)
    \(x_{\text {new }} \leftarrow \operatorname{Steer}\left(x_{\text {nearest }}, x_{\text {rand }}\right)\)
    if ObstacleFree \(\left(x_{\text {nearest }}, x_{\text {new }}\right)\) then
        \(X_{\text {near }} \leftarrow \operatorname{Near}\left(G, x_{\text {new }}, r, \eta\right)\)
        \(V \leftarrow V \cup\left\{x_{\text {new }}\right\} ; \quad x_{\text {rand }} \leftarrow x_{\text {nearest }}\)
        \(c_{\text {min }} \leftarrow \operatorname{Cost}\left(x_{\text {nearest }}\right)+c\left(\operatorname{Line}\left(x_{\text {nearest }}, x_{\text {new }}\right)\right)\)
    foreach \(x_{\text {near }} \in X_{\text {near }}\) do
        if CollisionFree \(\left(x_{\text {near }}, x_{\text {new }}\right) \wedge \operatorname{Cost}\left(x_{\text {near }}\right)+c\left(\operatorname{Line}\left(x_{\text {near }}, x_{\text {new }}\right)\right)<c_{\text {min }}\) then
            \(x_{\text {min }} \leftarrow x_{\text {near }} ; \quad \quad c_{\text {min }} \leftarrow \operatorname{Cost}\left(x_{\text {near }}\right)+c\left(\operatorname{Line}\left(x_{\text {near }}, x_{\text {new }}\right)\right)\)
        \(E \leftarrow E \cup\left\{\left(x_{\text {min }}, x_{\text {new }}\right)\right\}\)
    foreach \(x_{\text {near }} \epsilon X_{\text {near }}\) do
        if CollisionFree \(\left(x_{\text {new }}, x_{\text {near }}\right) \wedge \operatorname{Cost}\left(x_{\text {new }}\right)+c\left(\operatorname{Line}\left(x_{\text {new }}, x_{\text {near }}\right)\right)<\operatorname{Cost}\left(x_{\text {near }}\right)\) then
        \(x_{\text {parent }} \leftarrow \operatorname{Parent}\left(x_{\text {near }}\right)\)
        \(E \leftarrow\left(E \backslash\left\{\left(x_{\text {parent }}, x_{\text {near }}\right)\right\}\right) \cup\left\{\left(x_{\text {new }}, x_{\text {near }}\right)\right\}\)
```

return $G=(V, E)$

## Potentialised-RRT* Pseudo Code

```
Potentialised-RRT* ()
\(V \leftarrow\left\{x_{\text {init }}\right\} ; \quad E \leftarrow \phi\)
for \(i=1,2, \ldots, n\) do
    \(z_{\text {rand }} \leftarrow\) SampleFree \(_{i} ; \quad x_{\text {rand }} \leftarrow\) RandomisedGradientDescent \(\left(z_{\text {rand }}\right)\);
    \(x_{\text {nearest }} \leftarrow \operatorname{Nearest}\left(G, x_{\text {rand }}\right) ; \quad x_{\text {new }} \leftarrow \operatorname{Steer}\left(x_{\text {nearest }}, x_{\text {rand }}\right)\)
    if ObstacleFree \(\left(x_{\text {nearest }}, x_{\text {new }}\right)\) then
        \(X_{\text {near }} \leftarrow \operatorname{Near}\left(G, x_{\text {new }}, r, \eta\right)\)
        \(V \leftarrow V \cup\left\{x_{\text {new }}\right\} ; \quad x_{\text {rand }} \leftarrow x_{\text {nearest }}\)
        \(c_{\text {min }} \leftarrow \operatorname{Cost}\left(x_{\text {nearest }}\right)+c\left(\operatorname{Line}\left(x_{\text {nearest }}, x_{\text {new }}\right)\right)\)
    foreach \(x_{\text {near }} \epsilon X_{\text {near }}\) do
        if CollisionFree \(\left(x_{\text {near }}, x_{\text {new }}\right) \wedge \operatorname{Cost}\left(x_{\text {near }}\right)+c\left(\operatorname{Line}\left(x_{\text {near }}, x_{\text {new }}\right)\right)<c_{\text {min }}\) then
            \(x_{\text {min }} \leftarrow x_{\text {near }} ; \quad c_{\text {min }} \leftarrow \operatorname{Cost}\left(x_{\text {near }}\right)+c\left(\operatorname{Line}\left(x_{\text {near }}, x_{\text {new }}\right)\right)\)
        \(E \leftarrow E \cup\left\{\left(x_{\text {min }}, x_{\text {new }}\right)\right\}\)
    foreach \(x_{\text {near }} \epsilon X_{\text {near }}\) do
        if \(\operatorname{CollisionFree}\left(x_{\text {new }}, x_{\text {near }}\right) \wedge \operatorname{Cost}\left(x_{\text {new }}\right)+c\left(\operatorname{Line}\left(x_{\text {new }}, x_{\text {near }}\right)\right)<\operatorname{Cost}\left(x_{\text {near }}\right)\) then
            \(x_{\text {parent }} \leftarrow \operatorname{Parent}\left(x_{\text {near }}\right)\)
            \(E \leftarrow\left(E \backslash\left\{\left(x_{\text {parent }}, x_{\text {near }}\right)\right\}\right) \cup\left\{\left(x_{\text {new }}, x_{\text {near }}\right)\right\}\)
```

return $G=(V, E)$

## RandomisedGradientDescent Pseudo Code

```
RandomisedGradientDescent ( }\mp@subsup{z}{\mathrm{ rand }}{}\mathrm{ )
    (\nablaU Utt},\nabla\mp@subsup{U}{\mathrm{ rep }}{})\leftarrow\mathrm{ PotentialGradient (zrand}
    \alpha\leftarrowComputeStepSize( }\nabla\mp@subsup{U}{\mathrm{ att }}{},\nabla\mp@subsup{U}{\mathrm{ rep }}{},\mp@subsup{z}{\mathrm{ rand }}{}
    \nablaU\leftarrow-(\nablaU Utt + | U rep )
    D}\leftarrow\frac{(\nablaU)}{|\nablaU|
    x rand}\leftarrow\mp@subsup{z}{\mathrm{ rand }}{}+\alpha*\vec{D
    return }\mp@subsup{x}{\mathrm{ rand}}{
```

