

Distinguishing Cause and Effect

Balram Meena

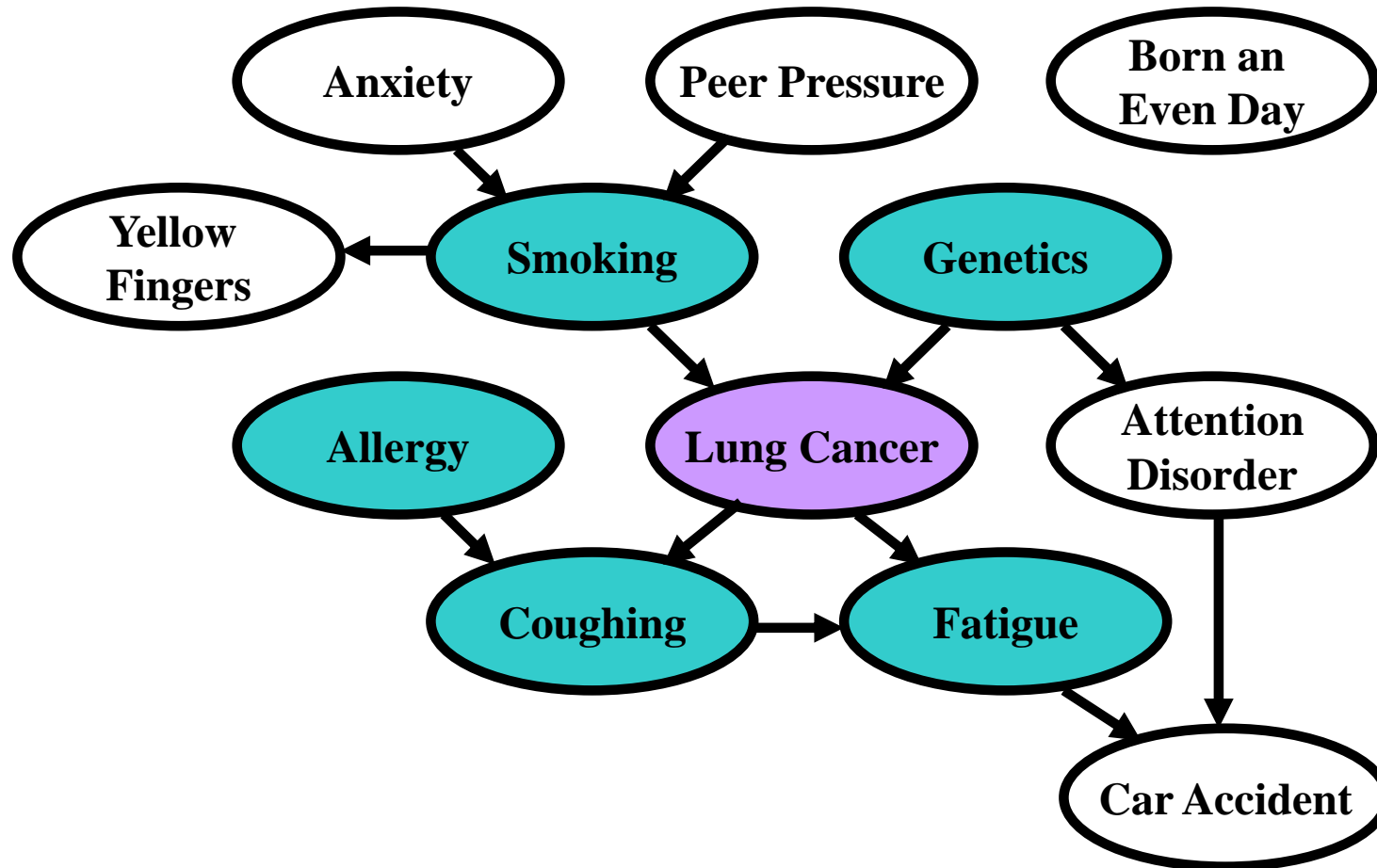
Lohit Jain

Indian Institute of Technology Kanpur

Motivation

- Pervasive in Science, Medicine, Economy and many aspects of everyday life.
- What affects Health, Economy, Climate Changes?
- Gold Standard: Randomized Controlled Experiments
- Experiments Costly, Unethical, Unfeasible!
- Non Observational Routine Data easily available

Causal Graph Example



Causality Challenge #3: Cause Effect Pairs

- Part of IJCNN 2013 contests
- Results discussed in NIPS 2013
- Proceedings: Journal of Machine Learning Research, Workshop and Conference Proceedings (JMLR)

Causality Challenge #3: Cause Effect Pairs

- Challenge: Rank pairs of variables $\{A, B\}$ to prioritize experimental verifications of the conjecture that A causes B.
- Determine from the joint observation of samples of two variables A and B that $A \rightarrow B$.
- But, “Correlation does not mean Causation”!
- Could be Consequences of a common cause.

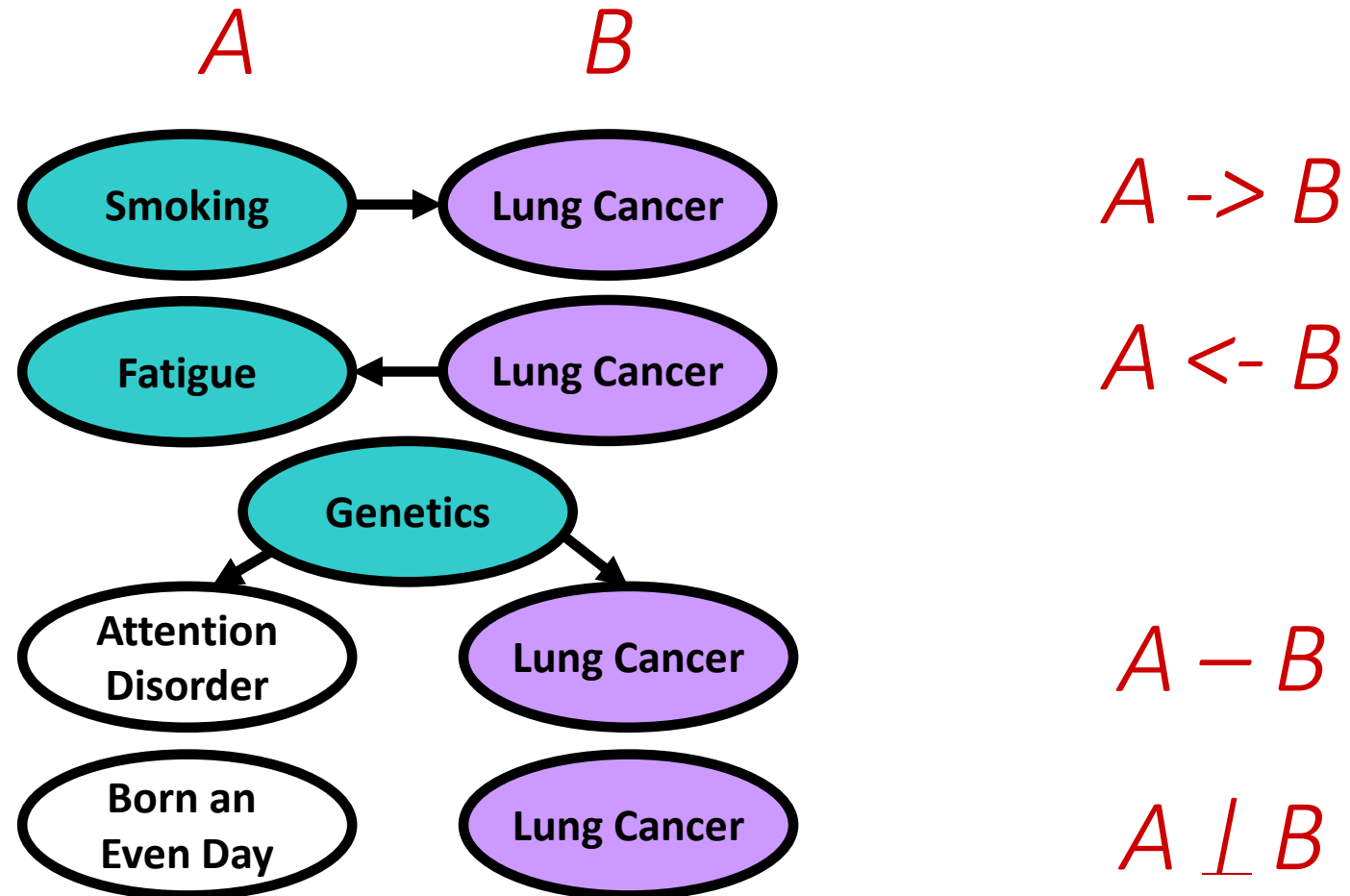
Setup

- No feedback loops.
- No Explicit time information
- Variables are aggregate statistic, eg: Temp, life expectancy.
- Pairs independent of each other

Datasets

- Pair of real variables intermixed with
 - controls (dependent but not causally related) and
 - semi-artificial cause-effect pairs (real variables mixed in various ways to produce a given outcome)
- 4050 training pairs
- 4050 validation pairs
- 4050 test pairs

Cause Effect Pair problem



Evaluation Scheme

- For any pair, score between $-\text{Inf}$ and $+\text{Inf}$,
- Large positive values : A is a cause of B with certainty
- Large negative values : B is a cause of A with certainty
- Near zero : Neither A causes B nor B causes A
- Scores as ranking criterion
- Evaluate entries with two *Area under the ROC Curve* (AUC) scores

Area Under the ROC curve

- The results of classification, obtained by thresholding the prediction score, may be represented in a confusion matrix, where tp (true positive), fn (false negative), tn (true negative) and fp (false positive) represent the number of examples falling into each possible outcome:
- We define the sensitivity (also called true positive rate or hit rate) and the specificity (true negative rate) as:
 - Sensitivity = tp/pos
 - Specificity = tn/negwhere $pos=tp+fn$ is the total number of positive examples and $neg=tn+fp$ the total number of negative examples.
- The area under the curve obtained by plotting sensitivity against specificity by varying a threshold on the prediction values to determine the classification result.
- The AUC is calculated using the trapezoid method.

Causality in two variables : Intuitively

- Intuitively : Factorization of the joint distribution
 $P(\text{cause}; \text{effect})$ into $P(\text{cause})P(\text{effect} \mid \text{cause})$
typically yields models of lower total complexity than
 $P(\text{cause}; \text{effect})$ into $P(\text{effect})P(\text{cause} \mid \text{effect})$
- Definition of Notion of Intuition not obvious!

Previous Models

- The methods define classes of conditionals \mathbf{C} and marginal distributions \mathbf{M} , and prefer
- $X \rightarrow Y$ whenever $P(X) \in \mathbf{M}$ and $P(Y | X) \in \mathbf{C}$
but $P(Y) \notin \mathbf{M}$ or $P(X | Y) \notin \mathbf{C}$.
- Notion of model complexity: all probability distributions inside the class are simple, and those outside the class are complex.
- This a priori restriction poses serious practical limitations

Causality in two variables

- Deterministic

$$f(X,E) = F(X)$$

- Non-deterministic

- I. AN(additive noise)

$$f(X,E) = F(X) + E$$

- II. PNL (Post-Non-Linear model)

$$f(X,E) = G(F(X) + E)$$

- III. LINGAM (f is linear)

$$f(X,E) = pX + qE$$

- IV. HS (hetero-Schedastic noise)

$$f(X,E) = F(X) + E.G(X)$$

- Idea is to fit restriction model in both direction ($X \rightarrow Y$ and $Y \rightarrow X$)
- Direction to be one that yields the best fit.

Probabilistic Latent Variable : Additional Assumptions

- A. Determinism (no other causes of Y): a function f exists such that $Y = f(X,E)$
- B. X and E are independent.
- C. The distribution of the cause is “independent” from the causal mechanism (f)
- D. The noise has a standard-normal distribution: $E \sim N(0,1)$

Other Models

- Based on (A) and (B) with some additional restrictions on f (Slide 13).
- For these special cases, it has been shown that a model of the same (restricted) form in the reverse direction $Y \rightarrow X$ that induces the same joint distribution on (X, Y) does not exist in general.
- But, a limited model class may lead to wrong conclusions about the causal direction.

Probabilistic Latent Variable Model

- In general, one can always construct a random variable $E' \sim N(0,1)$ and a $f' : \mathbb{R}^2 \rightarrow \mathbb{R}$ such that

$$X = f'(Y, E')$$

- In combination with (C) and (D) : an asymmetry!
- Infer the causal direction

Basic Idea

- Define non-parametric priors on the f and input distributions favoring lower complexity.
- Inferring using standard Bayesian model selection
- Preference to model with largest marginal likelihood
- Bayesian Approach: Noise as Latent Variable summarizing influence of all other unobserved causes.

Bayesian Model Selection

- Prefer model with highest evidence:

$$\rho(D|M) = \int \rho(D|\theta, M) \rho(\theta|M) d\theta,$$

D=Data, M=Model, θ =Parameters

Trade-off between likelihood (goodness of fit) and priors (model complexity).

- Causal Discovery: Compare evidence $X \rightarrow Y$ and $Y \rightarrow X$

References

- Mooij, Joris M., et al. "Probabilistic latent variable models for distinguishing between cause and effect." NIPS. 2010.
- Daniusis, Povilas, et al. "Inferring deterministic causal relations." arXiv preprint arXiv:1203.3475 (2012).
- Hoyer, Patrik O., et al. "Nonlinear causal discovery with additive noise models." NIPS. Vol. 21. 2008.
- Peters, Jonas, Dominik Janzing, and Bernhard Scholkopf. "Causal inference on discrete data using additive noise models." Pattern Analysis and Machine Intelligence, IEEE Transactions on 33.12 (2011): 2436-2450.
- Janzing, Dominik, et al. "Information-geometric approach to inferring causal directions." Artificial Intelligence 182 (2012): 1-31.

Thank You!

Questions ...